

Stellar Parameter Determination

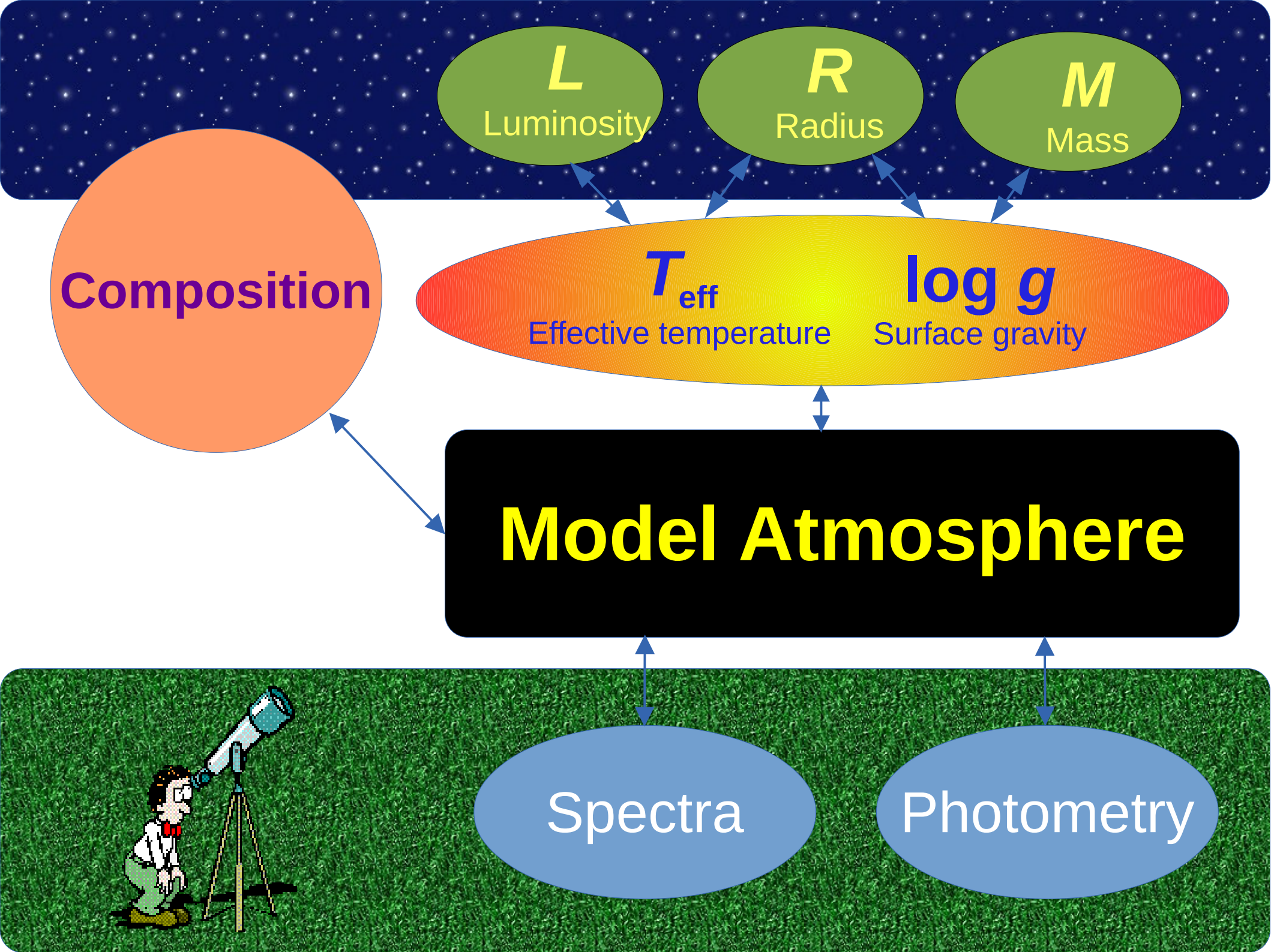
Barry Smalley

*Astrophysics Group
Keele University
Staffordshire ST5 5BG
United Kingdom*

b.smalley@keele.ac.uk



Keele University



L
Luminosity

R
Radius

M
Mass

Composition

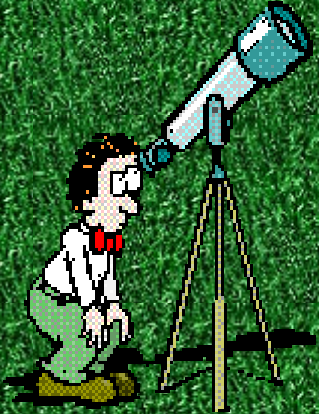
T_{eff}
Effective temperature

$\log g$
Surface gravity

Model Atmosphere

Spectra

Photometry



Effective Temperature

$$\sigma T_{eff}^4 \equiv \int_0^{\infty} F_{\nu} d\nu = F_{\star} = \frac{L}{4\pi R^2}$$

- Temperature of a black body that gives the same total power per unit area.
- Physically related to F_{\star} total radiant power per unit area at stellar surface.
- T_{eff} of star is temperature of blackbody with same luminosity and radius as the star

T_{eff} : Observable quantities

$$F_{\star} = \frac{\theta^2}{4} f_{\oplus}$$

- f_{\oplus} **total** flux at earth (UV, optical, IR)
 - **Corrected for interstellar reddening**
- θ is angular diameter
 - Directly: interferometry, lunar occultations
 - **Use limb-darkening corrected values**
 - Indirectly from eclipsing binary systems with known distances (parallaxes): $\theta \propto R/d \propto R \pi$

.. and asteroseismology !

Surface Gravity

Surface Gravity

Stellar Density

$$g = g_{\odot} M / R^2, \rho = \rho_{\odot} M / R^3 \quad g = R \rho = M^{1/3} \rho^{2/3}$$

- Directly given by stellar mass and radius.
 - An *indirect* measure of photospheric pressure
- Obtainable from:
 - Pairs (binary stars) **R and M**
 - Pulsations (asteroseismology) **ρ and R**
 - Planets (transits) **Just ρ (but need M or R)**

Fundamental Stars

- Fundamental stars can give accurate values of T_{eff} and $\log g$ for selected stars only.
 - Except for the Sun, good to no better than 1~2 %
- Composition is *not directly* measured
 - Closest is the Sun via solar system material
 - Fe 7.50 ± 0.04 (photosphere) 7.45 ± 0.01 (meteorites)
Asplund et al., 2009, ARA&A, 47, 481

Everything else is model dependent!

F,G and K Reference Stars

- For example, the GAIA Benchmark Stars
 - 34 Stars with well determined parameters
 - **Not all have fundamental T_{eff} and log g.**
 - Blanco-Cuaresma et al., 2014, A&A, 566, A98;
 - Jofre et al. 2014, A&A, 564, 133

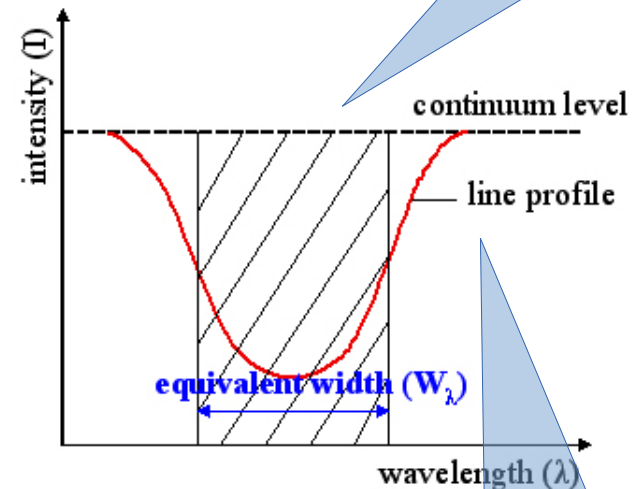
Indirect Methods

- Direct determination is usually impractical for most stars.
- Have to use indirect methods:
 - Photometric calibrations
 - Infrared Flux Method
 - Spectrophotometric flux fitting
 - Balmer Profiles
 - Line ratios
 - Equivalent Width Analysis
 - Spectrum Synthesis

Equivalent Width

Small errors in continuum can lead to relatively large errors in EW

- Measure of number of absorbers
 - Abundance
 - No information on profile shape
- Measure EWs of spectral lines
 - Manually
 - Automatically (ARES, DAOSPEC)



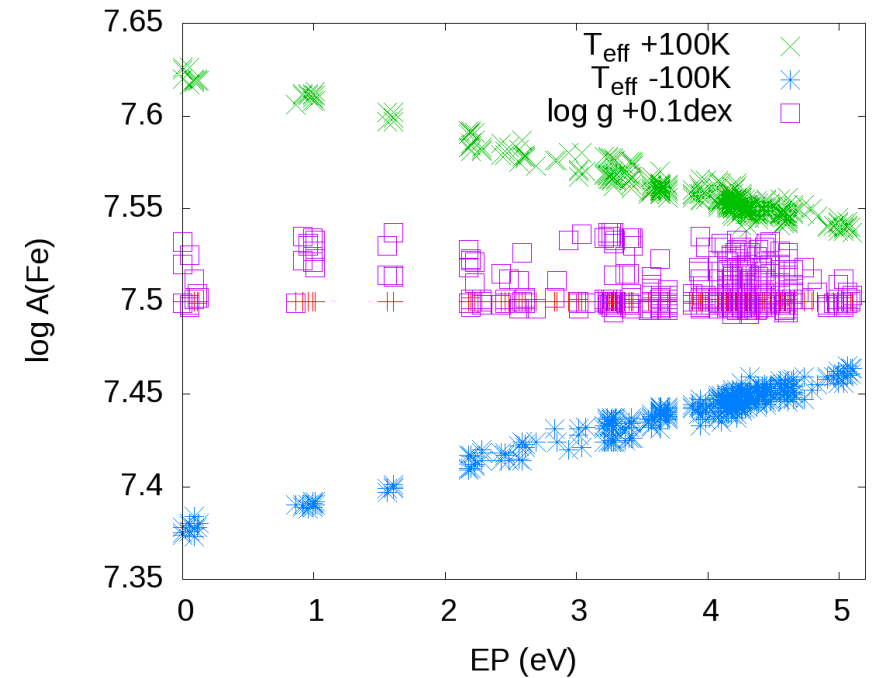
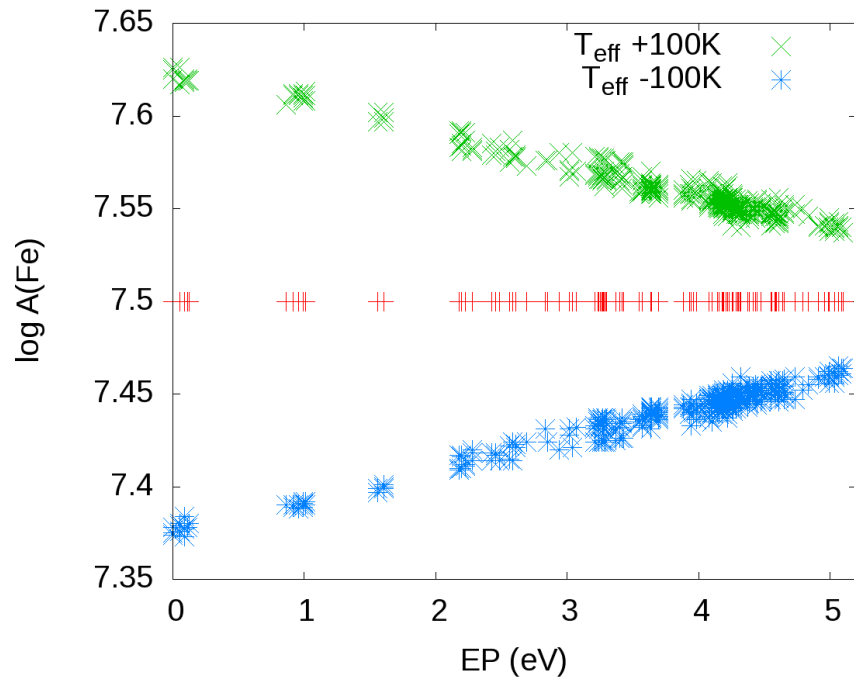
$$W_\lambda = \int_0^\infty (1 - F_\lambda / F_0) d\lambda$$

- Avoid strong lines with wings
- Profile truncation leads to underestimated EW

Metal Line Diagnostics

- log A versus Excitation Potential (T_{eff})
 - Abundances from the same element should agree for all excitation potentials, i.e. no trend
- log A versus EW (microturbulence)
 - Adjust V_{micro} until no trend with EW
- Ionization Balance ($\log g$)
 - Average log A obtained from differing ionization stages of the same element must agree
 - Fe I/Fe II ratio can be used as a $T_{\text{eff}} - \log g$ diagnostic

Effect of changing parameters



Simulation
Base model
 $T_{\text{eff}} = 6000\text{ K}$
 $\log g = 4.5$
 $\log A(\text{Fe}) = 7.50$

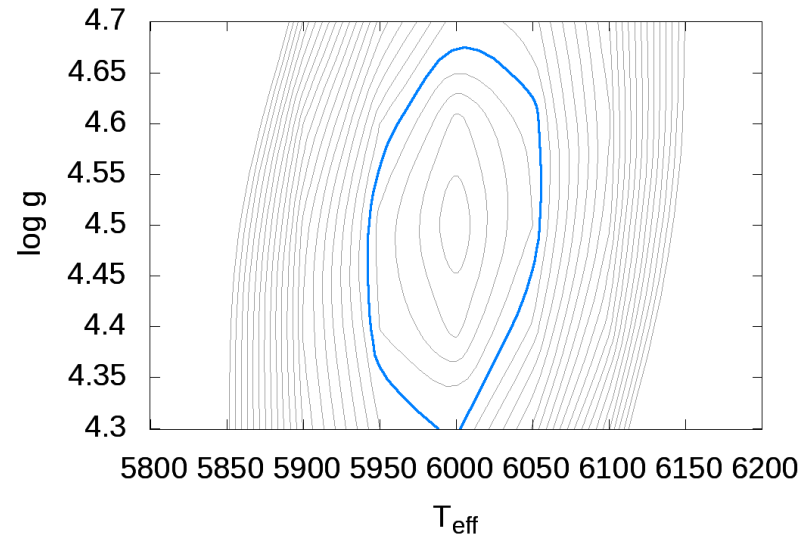
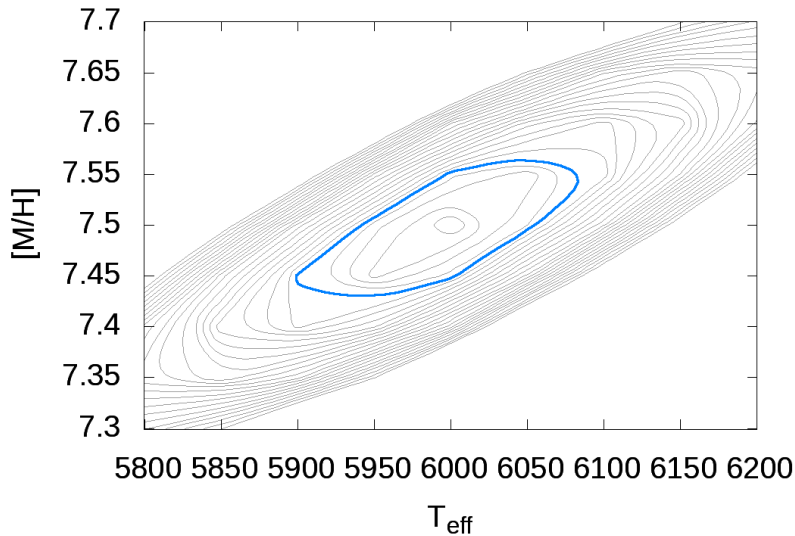
Fe I lines (not pressure sensitive in Solar-type stars)
Wavelength range 5000-6000Å
 $5 < \text{EW} < 100\text{ mÅ}$ (avoid very weak or saturated lines)

Spectral Fitting

- Measuring equivalent widths might not always be practical.
 - Blending, high rotation, etc.
- Take all or selected parts of spectrum
- Vary input parameters and calculate synthetic spectrum.
- Fit best fitting solution (minimize χ^2)
 - Error estimates are usually just internal precision

What about missing or incorrect line data?

χ^2 Correlations



- Correlation between [M/H] and T_{eff}
- Weak sensitivity to $\log g$

Simulation
Base model
 $T_{\text{eff}} = 6000$ K
 $\log g = 4.5$
 $\log A(\text{Fe}) = 7.50$

Generated with all lines with $\text{EW} > 5\text{m}\text{\AA}$
in wavelength range $5000\text{-}6000\text{\AA}$

Assumed S/N 100:1 for χ^2 calculation

A complex stellar recipe

- **Atomic/Molecular data**
 - Log gf , damping constants, missing/bad lines, hyperfine structure, isotopes
- **Atmospheric Physics**
 - NLTE, convection, turbulence, spots, abundance clouds
- **Modelling Code internals**
 - Partition functions, continuous opacities, numerical precision
- **Analysis Methods**
 - Equivalent widths, profile fitting, choice of lines and wavelength regions
- **Data Quality**
 - S/N, scattered light, continuum normalisation, telluric/interstellar lines
- **Stellar properties**
 - Binarity, variability

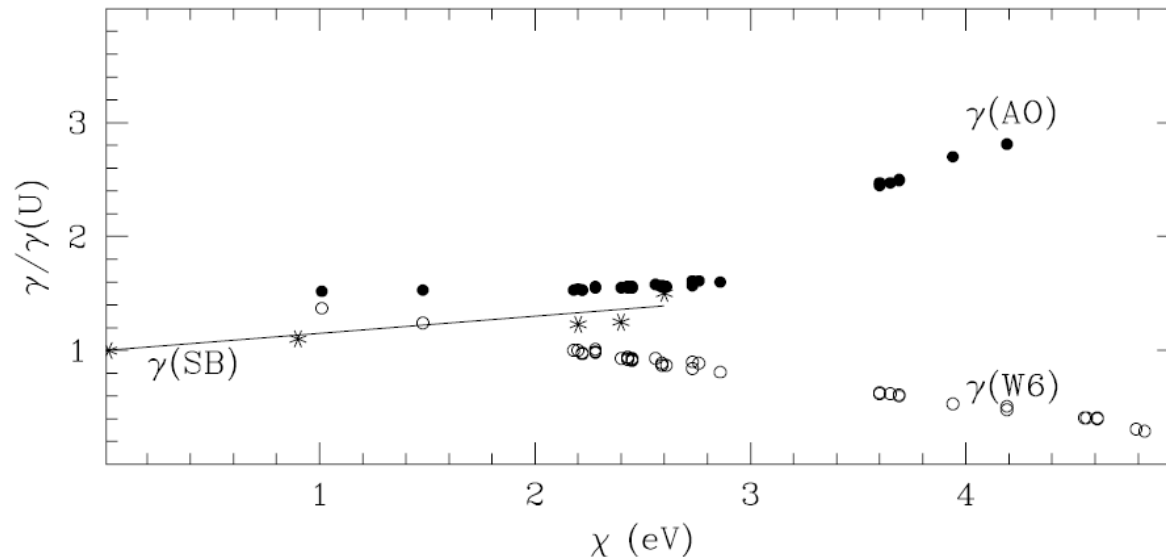


Plus other ingredients!

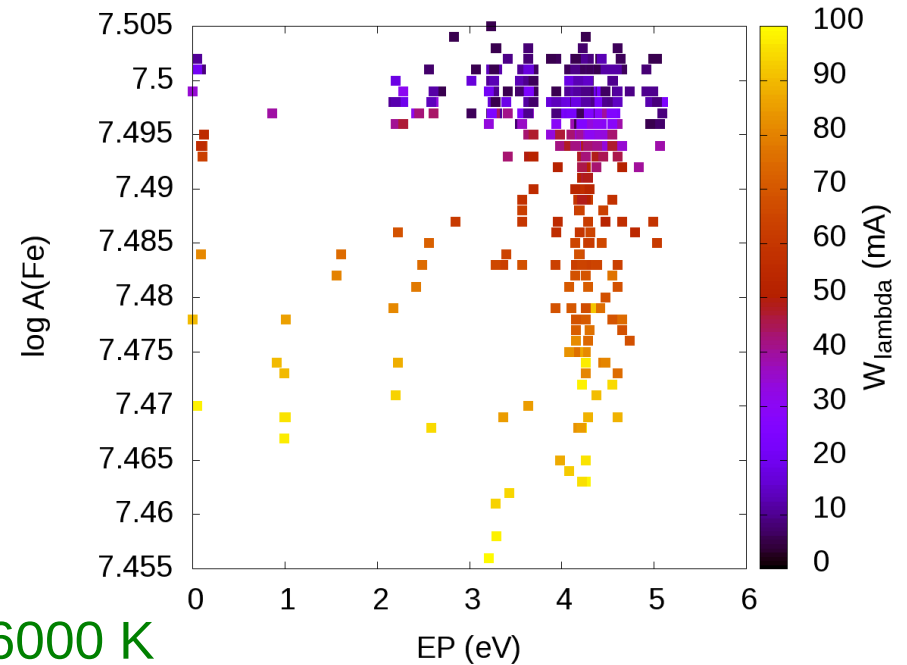
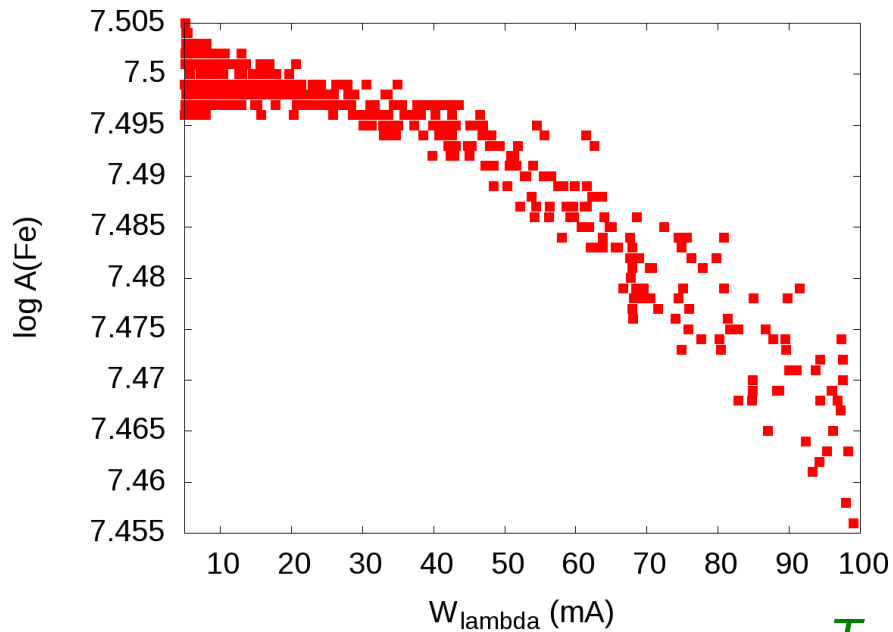
Pedagogical Heuristic Simulations

Collisional Broadening

- Ryan 1998 ([A&A, 331, 1051](#))
 - Even weak lines can be affected by damping
 - Damping errors depend on excitation potential
 - errors in v_{mic} and T_{eff}



Effect of damping



$T_{\text{eff}} = 6000 \text{ K}$

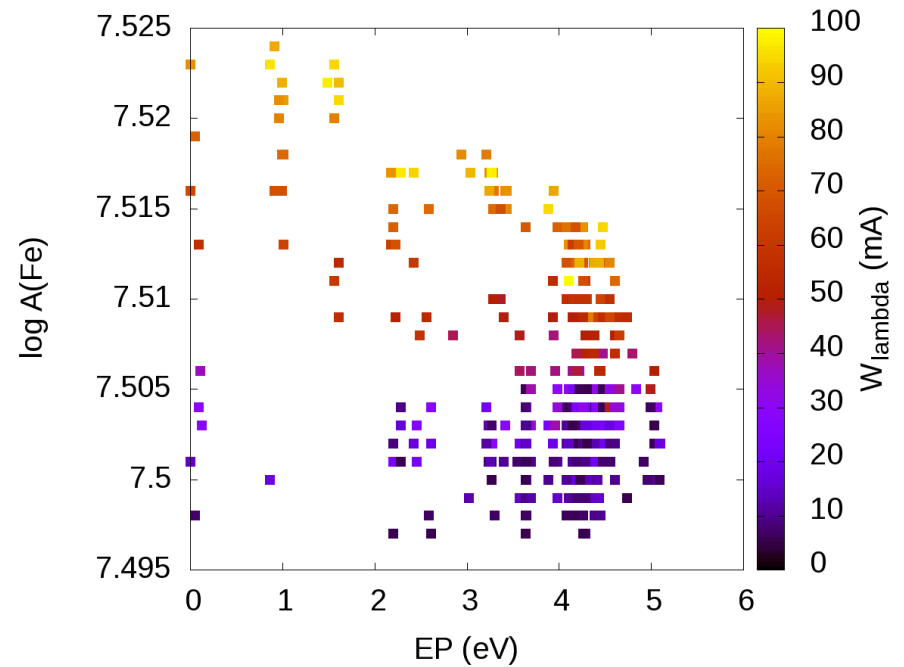
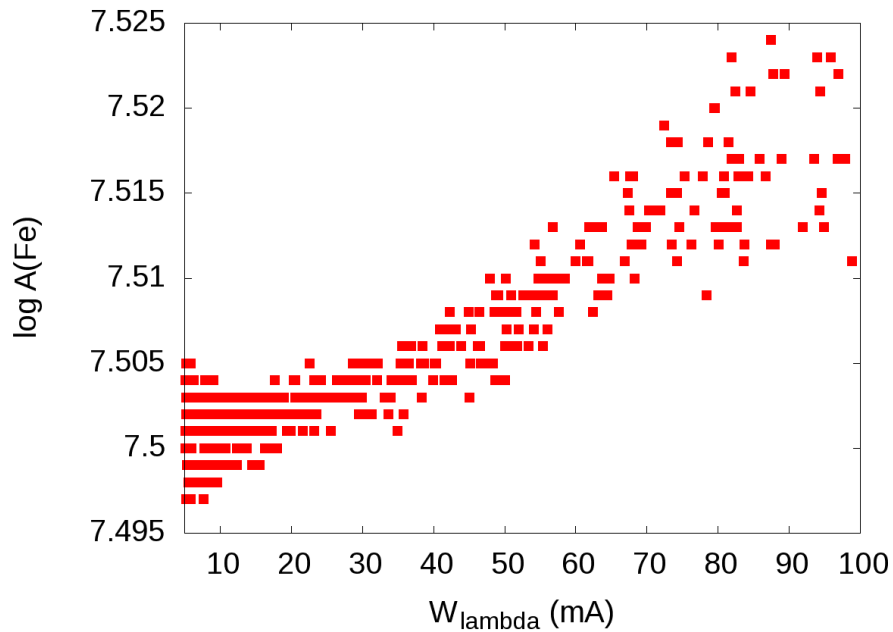
$\text{Log } g = 4.5$

- Effect of +20% error in van der Waals damping constant
 - could lead to errors in microturbulence and T_{eff}

Astrophysical gf values

- Line data is often inaccurate or missing
- Take spectrum of star with known properties and adjust synthesis line data until fits
 - Usually the Sun for late-type stars
 - Assume abundances are known
 - Mostly adjust just oscillator strengths (gf values)
- Widely-used and can give good results
 - **But** values do depend on model and assumed parameters.
 - Damping constants, microturbulence, convection, ...

Astrophysical *gf* Systematics

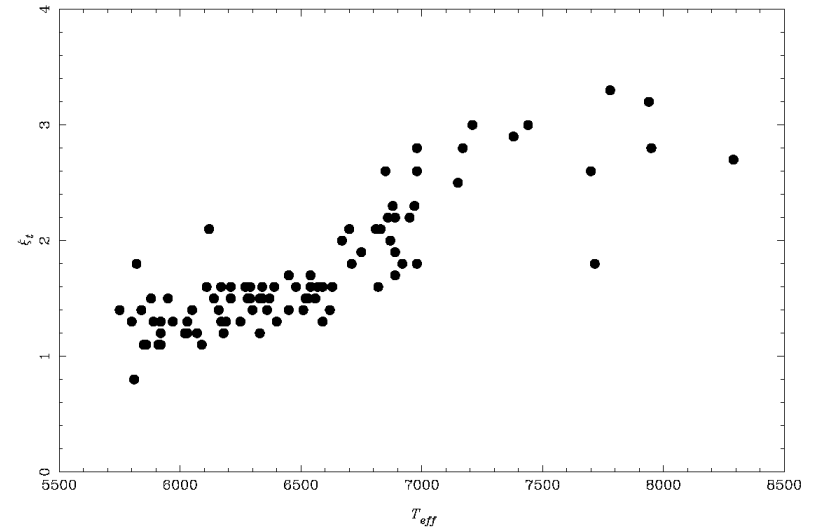


- Astrophysical *gf* values created at 6000 K but with +20% error in van der Waals damping.
 - Plots show difference in at 6500 K.

Not need in 3-d
simulations

Microturbulence

- A **free** parameter introduced to ensure that abundances from weak and strong lines agree
- Extra source of line broadening
 - added to thermal broadening
 - Small scale motions within the atmosphere



Smalley 2004, IAUS 224, 131 based on Gray et al. 2001, AJ, 121, 2159

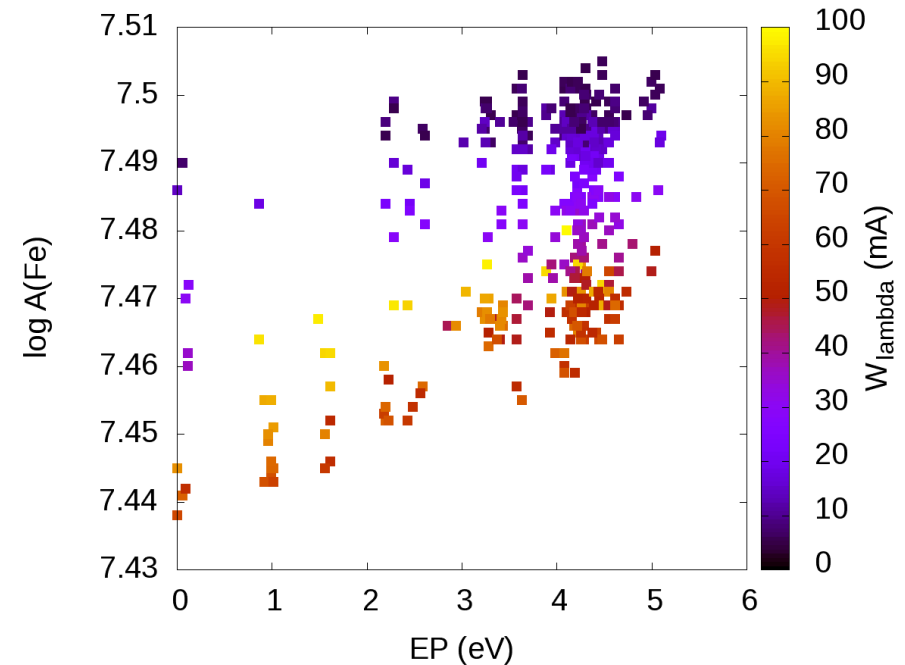
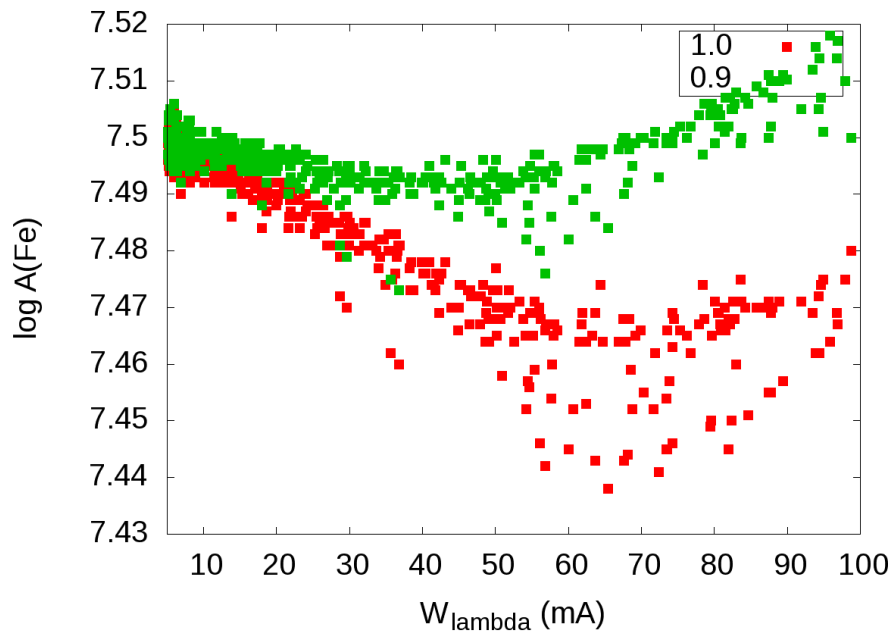
- Microturbulence varies with T_{eff}
 - increases with increasing temperature
 - peaking around mid-A type

Solar Microturbulence Value

- Edvardsson et al. 1993 (*A&A*, 275, 101) 1.15 km/s
- Bruntt et al. 2010 (*MNRAS*, 405, 1907) 0.95 km/s
- Valenti & Fischer 2005 (*ApJS*, 159, 141) 0.85 km/s
- Santos et al. 2004, (*A&A*, 415, 1153) 1.00 km/s
- Magain 1984 (*A&A*, 134, 189) 0.85 km/s (centre of solar disk)
 - From Blackwell et al. 1984, (*A&A*, 132, 236) using Holweger & Mueller 1974, (*SoPh*, 39, 19) Solar model

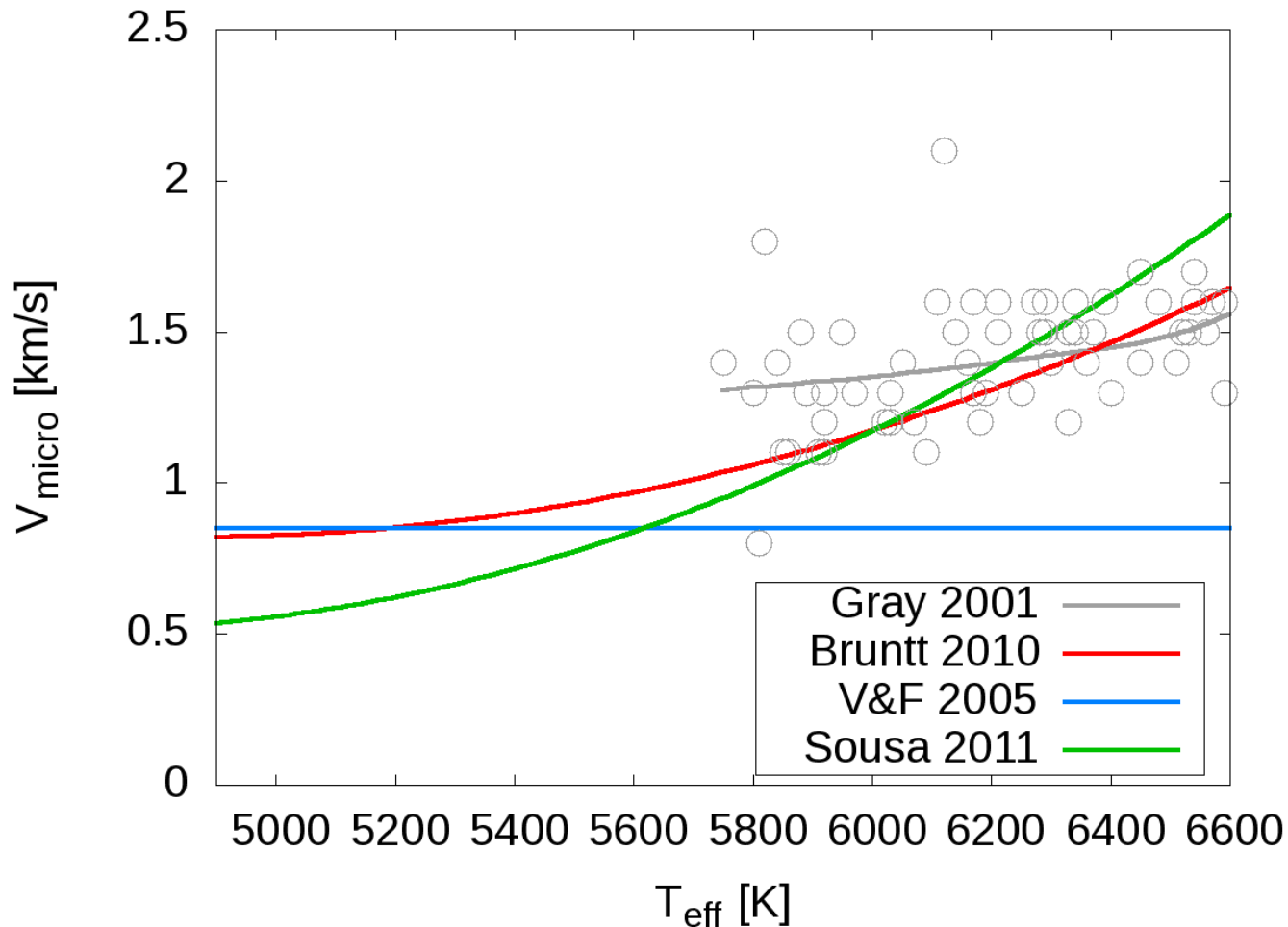
Which to use in Astrophysical *gf* determination?

Astrophysical gf Systematics



- Astrophysical gf values created at 6000 K but with microturbulence too low by 0.1 km/s.
 - 0.9 km/s instead of “true” 1.0 km/s
 - Plots show difference at 6500 K

Microturbulence Calibrations



Valenti & Fischer
2005 found:

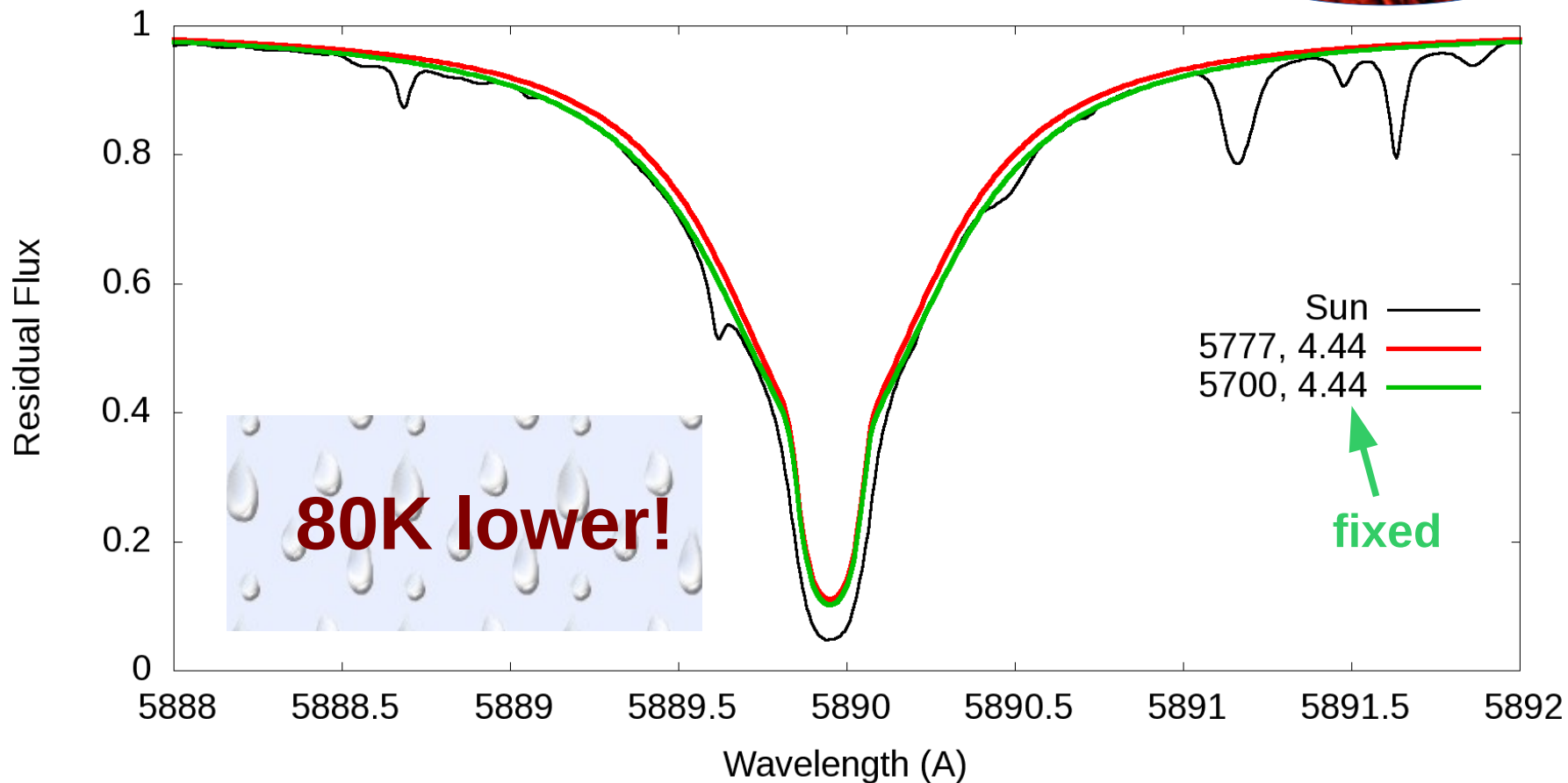
“strongly correlated
values of v_{mic} and
[M/H], suggesting
that v_{mic} and [M/H]
are partially
degenerate.”

Adopted fixed value.

Gray 2001 fit by Smalley 2004, IAUS, 224, 131
Sousa 2011 is fit given in 2013, ApJ, 768, 79

Valenti & Fischer, 2005, ApJS, 159, 141
Bruntt et al., 2010, MNRAS, 405, 1907

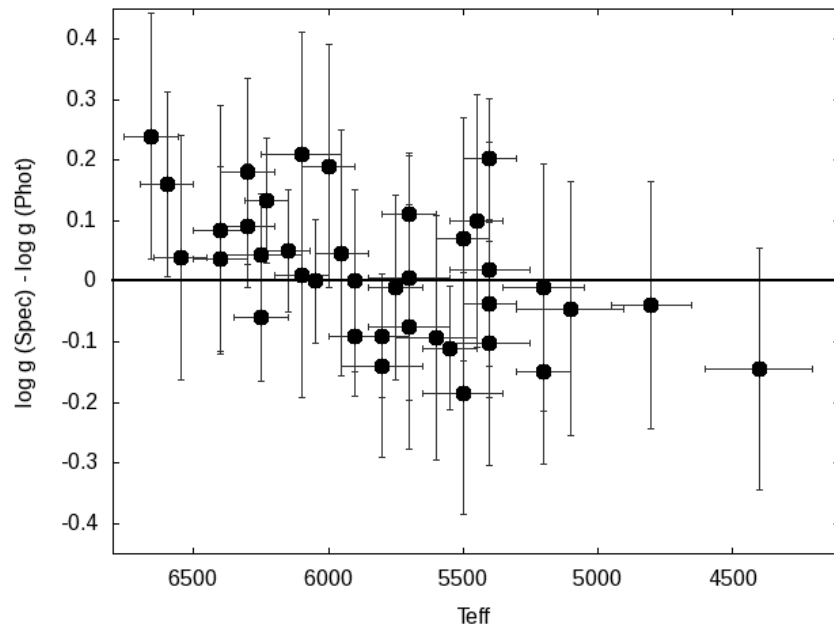
Fixing $\log g$



Fixing $\log g$ can lead to incorrect other parameters

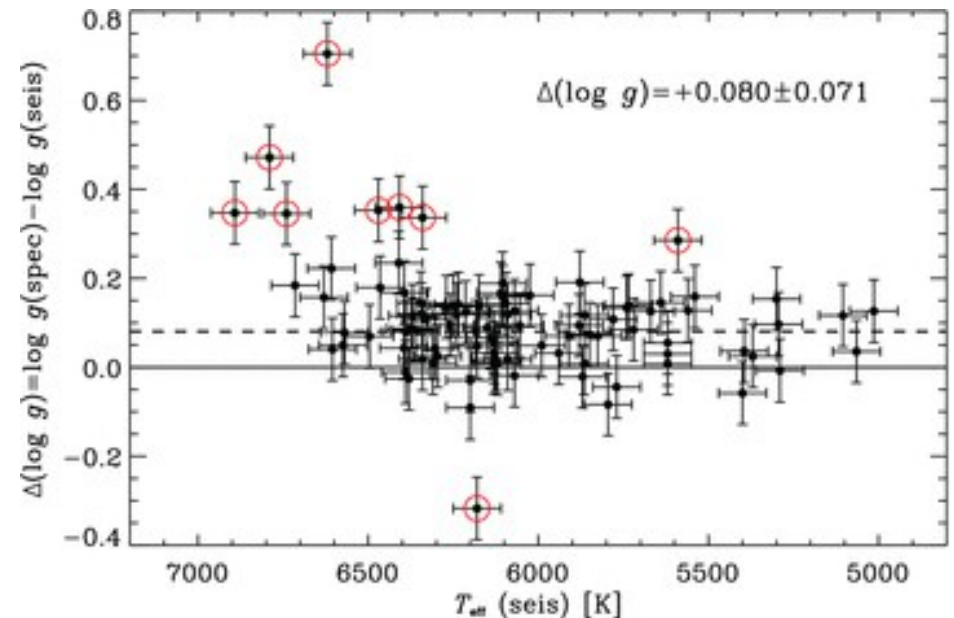
Surface Gravity from Spectroscopy

Transit log g



Smalley et al. 2012 A&A, 547, A61

Asteroseismic log g



Bruntt et al. 2012 MNRAS, 423, 122

Spectroscopic log g can be **accurately** determined to ± 0.1 dex
by spectral analysis alone!

Starspots

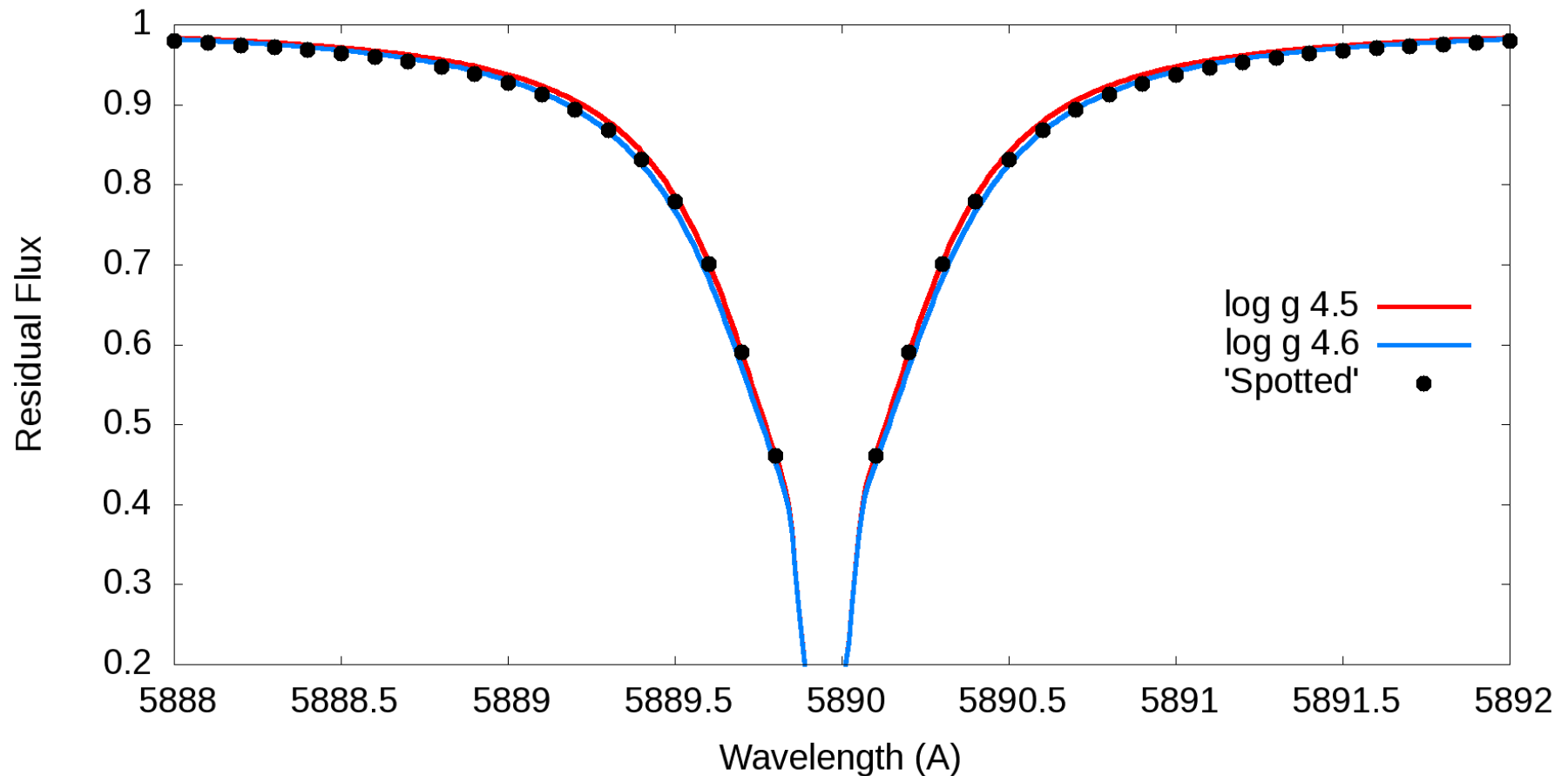
- Simulate a spotted star with 5% spot coverage.
- Take two models: $T_{\text{eff}} = 6000$ K and $T_{\text{eff}} = 5000$ K
 - Both with $\log g = 4.5$
- Generate spectra and combine 95% and 5%
- Fit with single T_{eff} model
- H_{α} gives 5950 K. Agrees with Stefan's Law:

$$(0.95 \times 6000^4 + 0.05 \times 5000^4)^{1/4} = 5953$$

- But, what $\log g$ does Na D give?

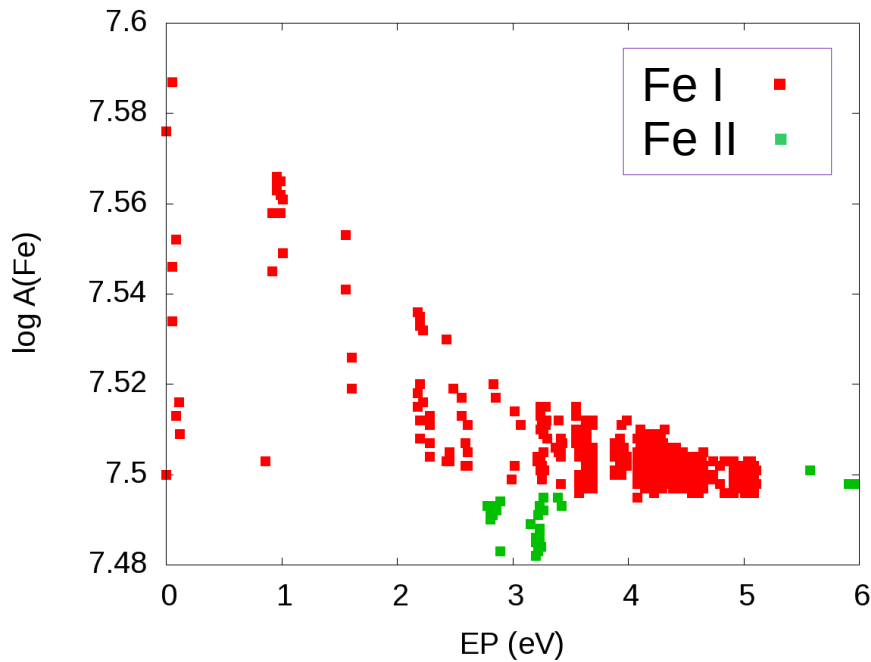


Effect of “Spot” on Na D line

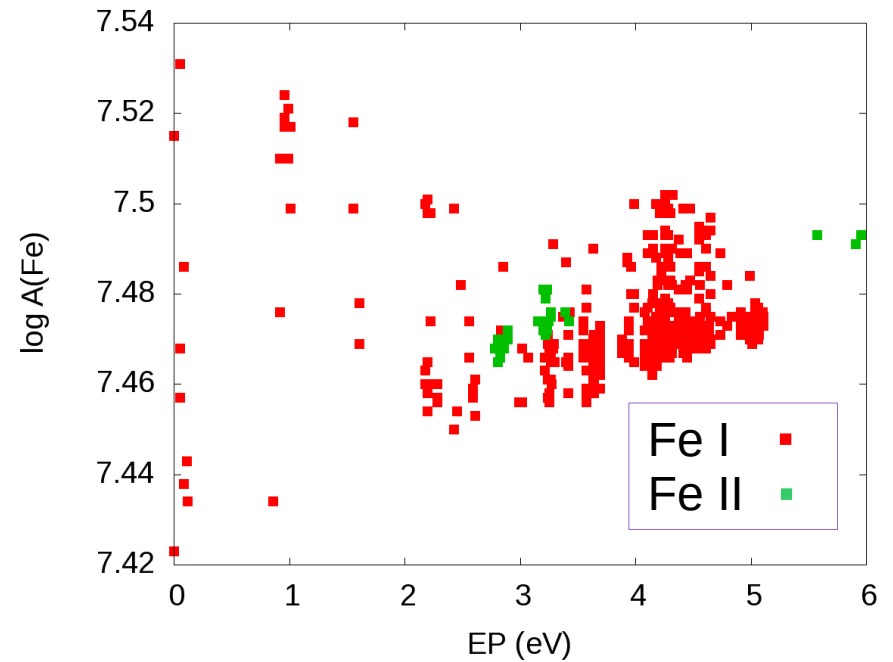


Spectroscopic $\log g$ overestimated in spotted stars?

Spots and EWs



$T_{\text{eff}} = 5953 \text{ K}$, $\log g = 4.5$



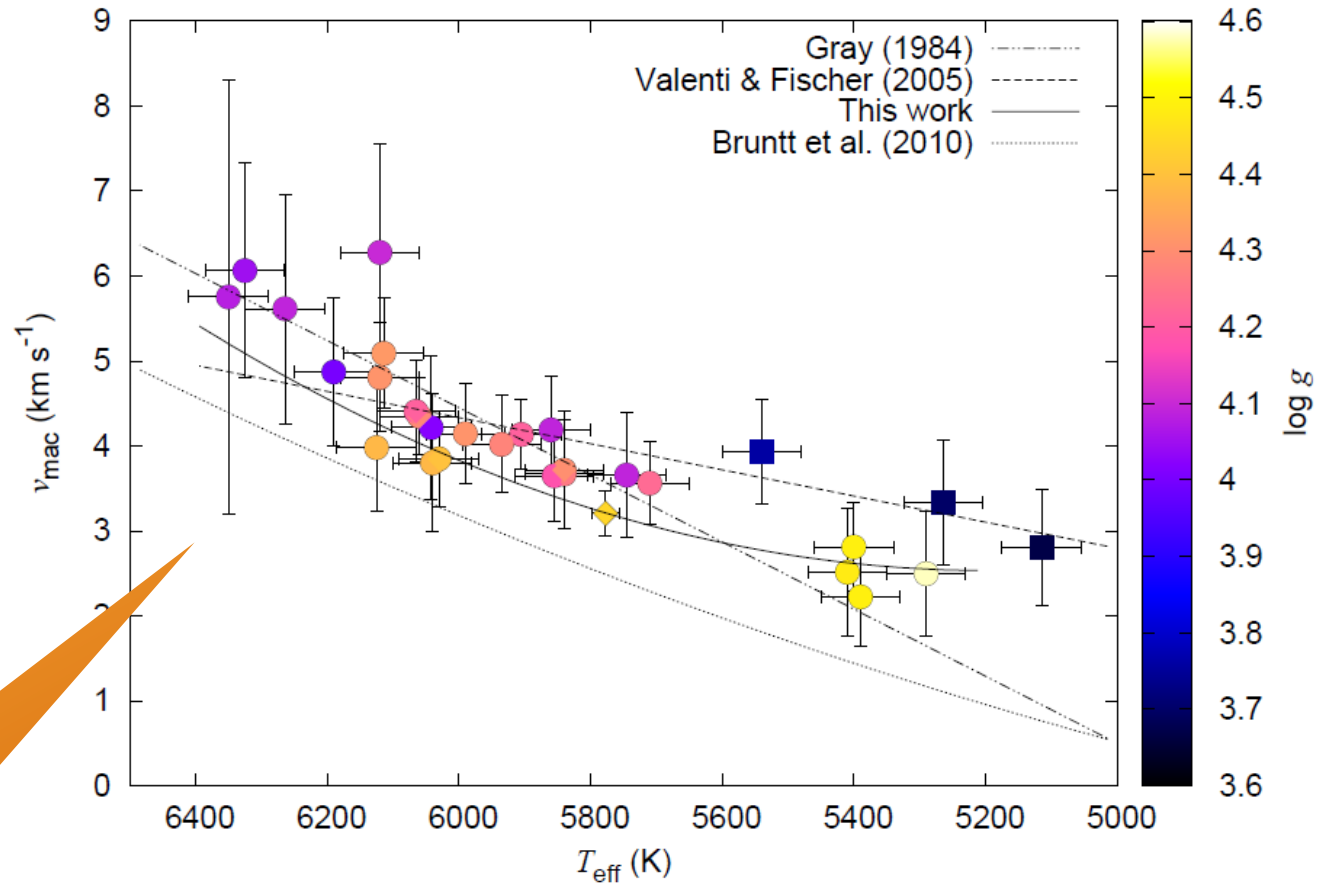
$T_{\text{eff}} = 5890 \text{ K}$, $\log g = 4.42$

- Effect on determination of T_{eff} and $\log g$
 - depends on choice of lines.

Macroturbulence

Stellar granulation

Difficult to disentangle between $v \sin i$ and macroturbulence on line profile



Base on $v \sin i$ from Kepler asteroseismology

Doyle et al. 2014 ArXiv 1408.3988

A few Case Studies from the Literature

WASP-13

SPECTROSCOPICALLY-DETERMINED STELLAR PARAMETERS OF WASP-13

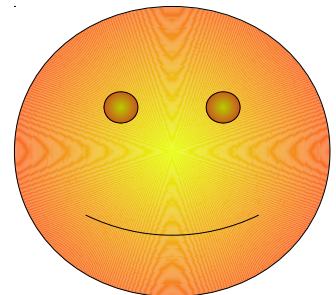
		SME	EW/ UCLSYN	ARES/ MOOG	ARES/ MOOG	Weighted Mean*
Unconstrained						
<i>T</i> _{eff} (K)	106	6003 ± 65	5955 ± 75	5919 ± 30	6025 ± 21	5989 ± 16 ± 48
log <i>g</i>	0.17	4.16 ± 0.08	4.13 ± 0.11	4.02 ± 0.06	4.19 ± 0.03	4.16 ± 0.03 ± 0.07
log <i>A</i> (Fe)	0.06	7.54 ± 0.06 [†]	7.60 ± 0.09	7.54 ± 0.05 [†]	7.58 ± 0.05 [†]	7.56 ± 0.03 ± 0.03
[Fe/H]		0.04 ± 0.05	0.10 ± 0.09 [†]	0.04 ± 0.02	0.08 ± 0.02	0.06 ± 0.01 ± 0.03
<i>v</i> sin <i>i</i> (km s ⁻¹)		5.79 ± 0.08	5.26 ± 0.25	5.74 ± 0.08 ± 0.38
<i>v</i> _t (km s ⁻¹)		1.01 ± 0.17 [‡]	0.95 ± 0.10	1.53 ± 0.09	1.28 ± 0.10	1.27 ± 0.06 ± 0.29

- H_α 5950 ± 70 K; log *g* (Transit) 4.10 ± 0.04
- SPC: 5982 ± 50 K (Torres et al. 2012, ApJ, 757, 161)
- IRFM: 5935 ± 183 K

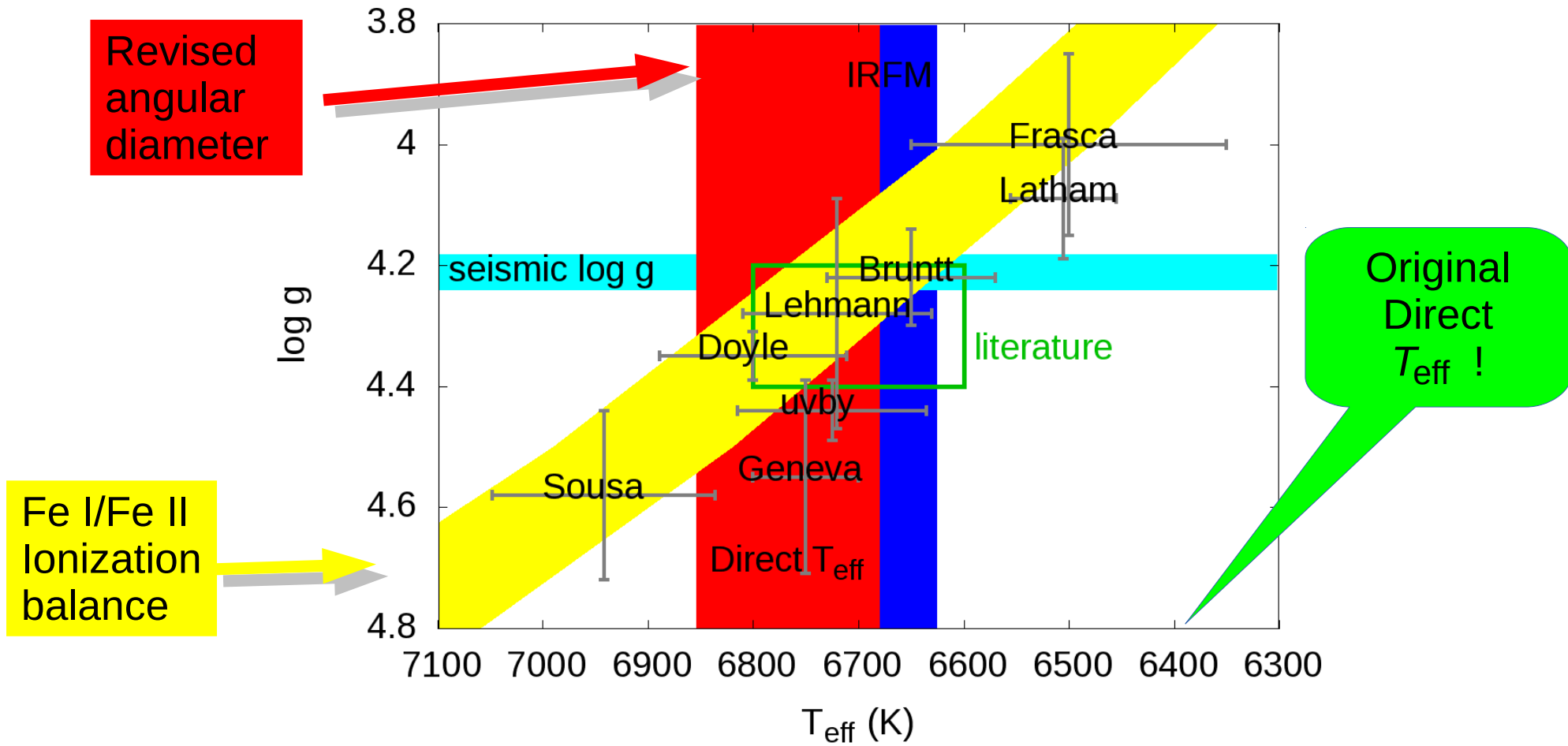
Gaia-ESO Survey

- The analysis of 1301 FGK-type stars ([2014arXiv1409.0568S](#))
- 13 independent groups and methods
 - All using MARCS models (no Kurucz ATLAS models)
- *Method-to-method dispersion* of the atmospheric parameters
 - T_{eff} 55 K, $\log g$ 0.13 dex, $[\text{Fe}/\text{H}]$ 0.07 dex
- *Systematic biases* are estimated to be between
 - T_{eff} 50-100 K, $\log g$ 0.10-0.25 dex, $[\text{Fe}/\text{H}]$ 0.05-0.10
- The typical method-to-method dispersion of elemental abundances varies between 0.10 and 0.20 dex.

**All spectral analysis methods are well developed
and yield satisfactory results**



Θ Cygni



Guzik et al. In prep

Summary

- Analyses should include sufficient reference stars
 - use exactly the same methods and quality of spectra.
- Use as many diagnostics as possible
 - Spectroscopic and photometric.
- Realistically the typical errors:
 - $T_{\text{eff}} \pm 50\sim 100\text{K}$
 - $\log g \pm 0.1\sim 0.2 \text{ dex}$
 - Abundances $\pm 0.05\sim 0.10 \text{ dex}$

Errorbars in stellar analyses *usually* show how well the model fits to the data and **not** how good is the model.

High precision fitting to high S/N data is possible, but overall accuracy of parameters is less certain.