

Planet Traps & Super-Earths

: Origins of the Planet-Metallicity Relation

& Implications for the Mass-Radius Diagram

Yasuhiro Hasegawa (EACOA fellow @ ASIAA / NAOJ)

Ralph Pudritz (McMaster Univ.)

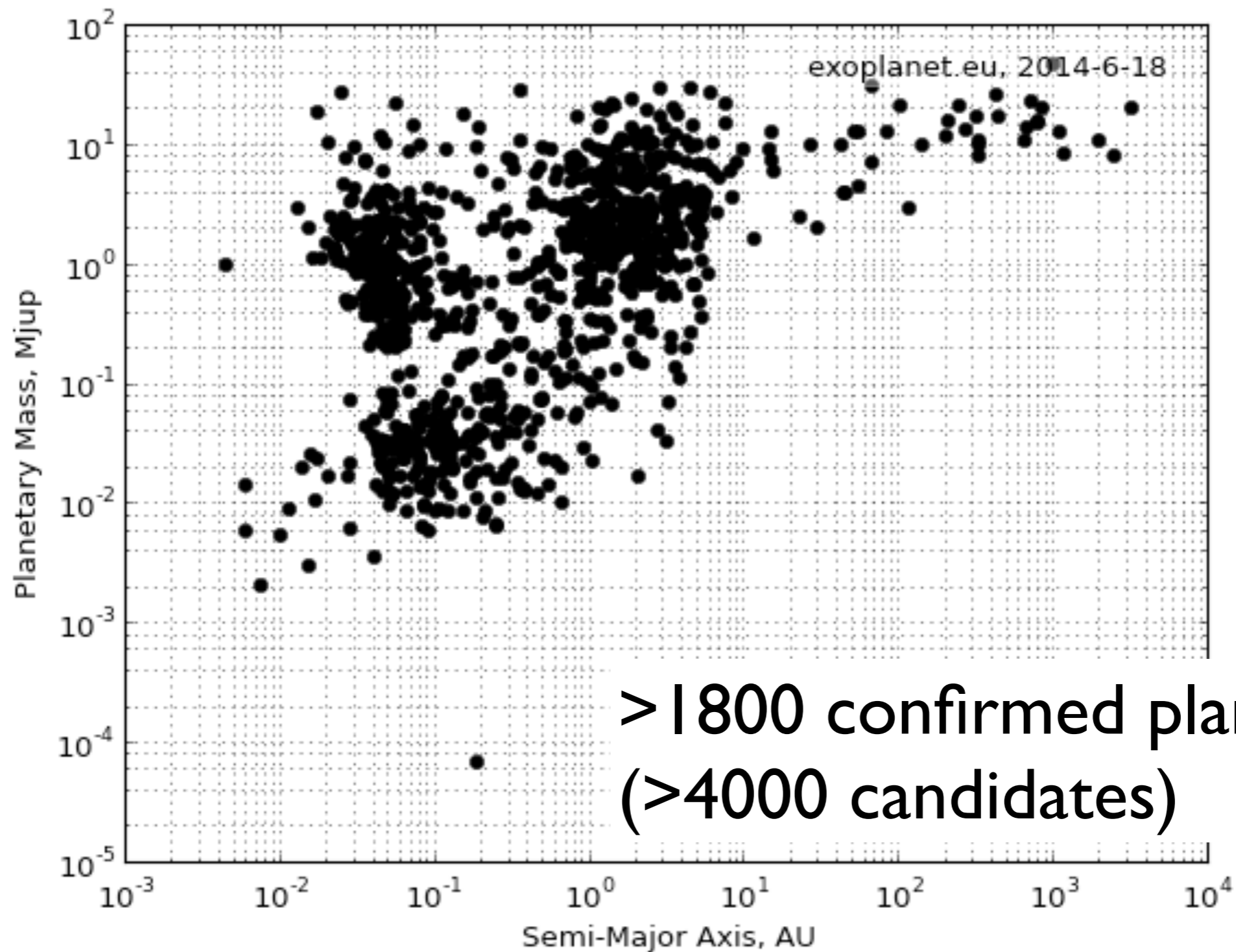
Planet Traps & Super-Earths

: Origins of the Planet-Metallicity Relation
=> see arXiv:1408.1841 (accepted by ApJ)

& Implications for the Mass-Radius Diagram

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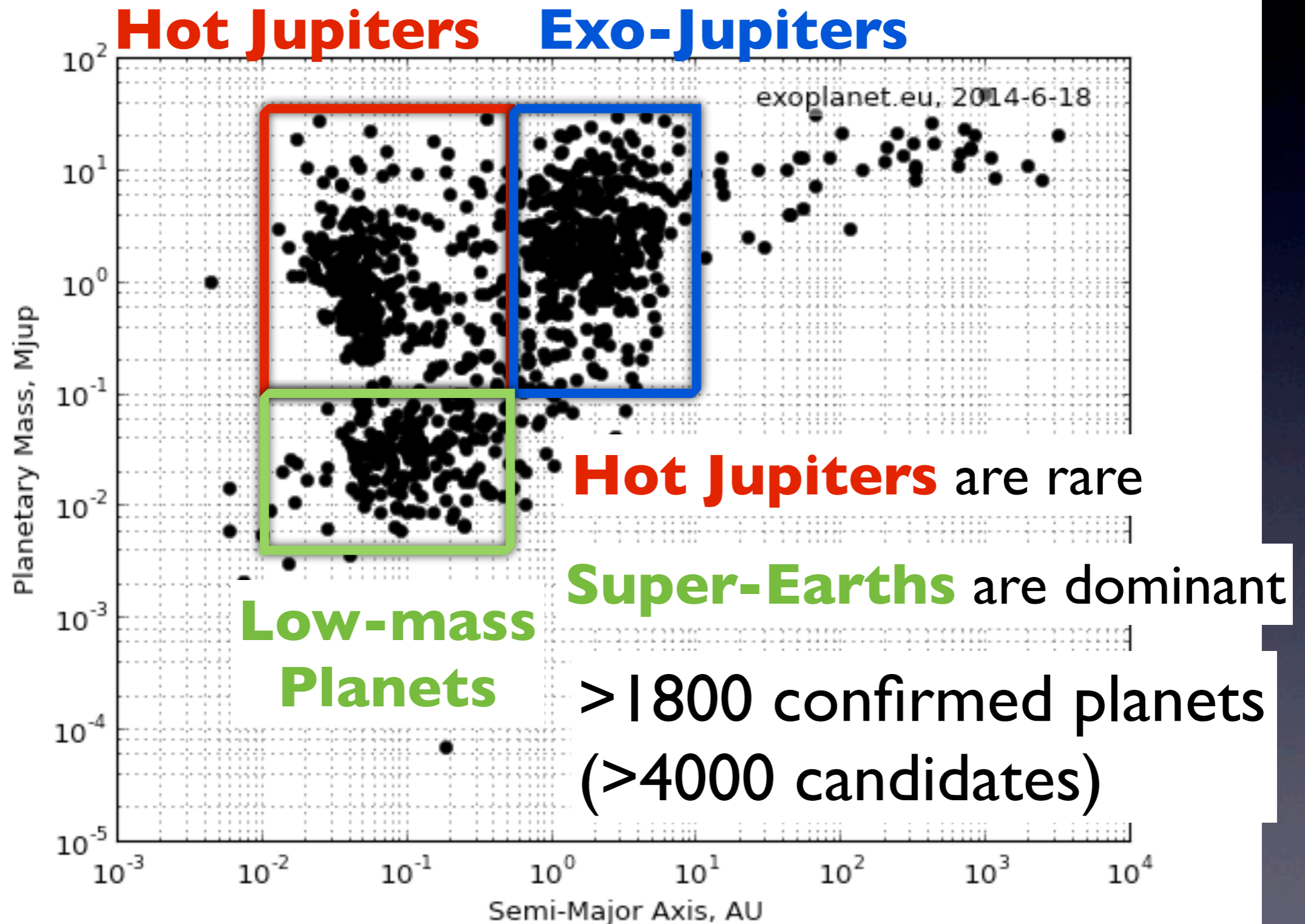
Mass-Semimajor Axis Diagram



**> 1800 confirmed planets
(>4000 candidates)**

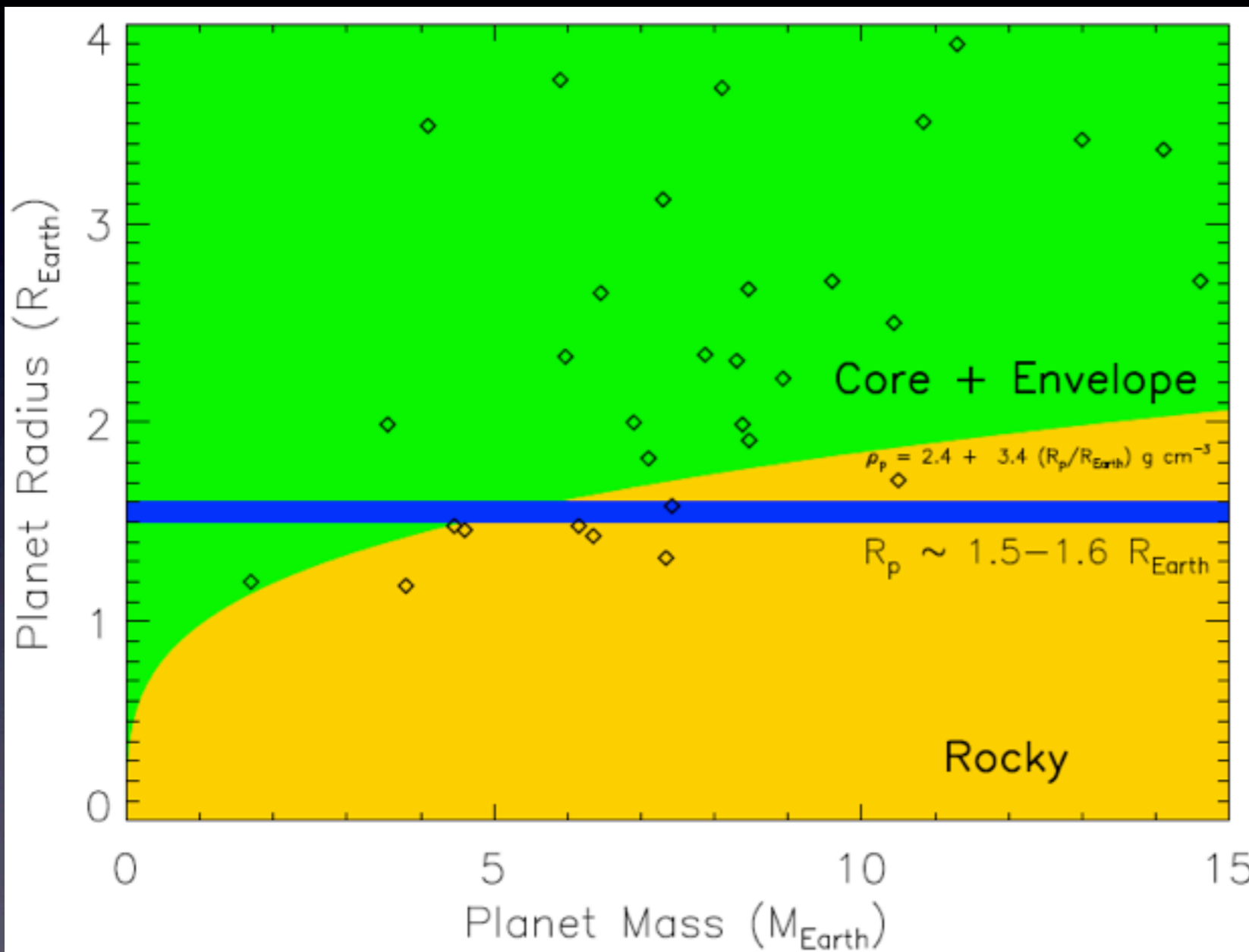
Distinct Populations

Chiang & Laughlin 2013, Hasegawa & Pudritz 2013, 2014



Mass-Radius Diagram

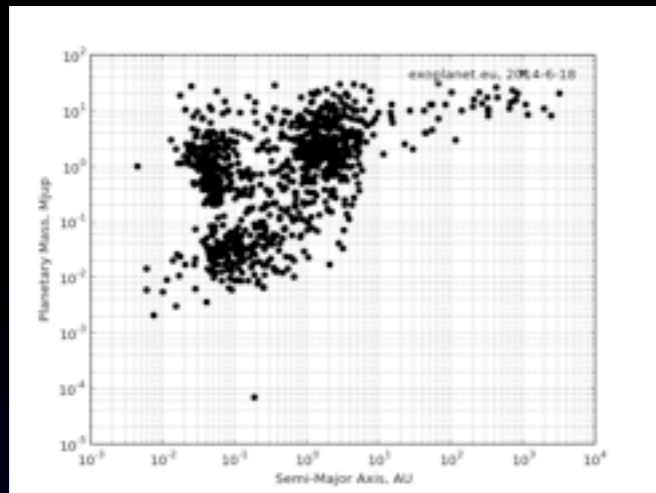
e.g., Weiss & Marcy 2014, Marcy et al 2014,
Rogers 2014, Wolfgang & Lopez 2014



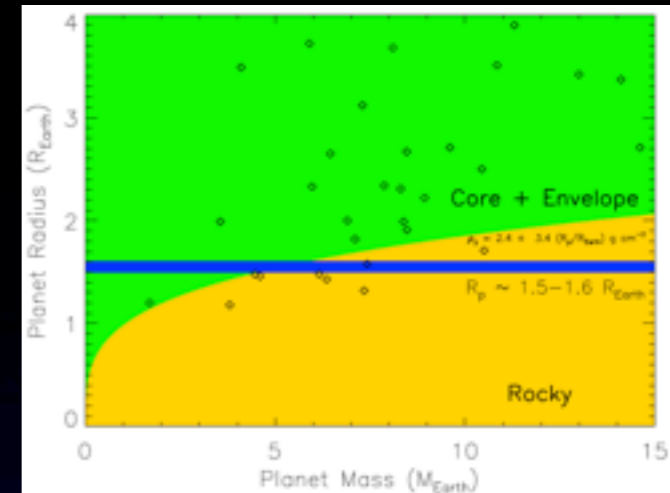
**Planets w/
 $> 1.5 - 1.6 R_{\text{Earth}}$
: not purely rocky**

**Planets w/
 $< 1.5 - 1.6 R_{\text{Earth}}$
: likely to be purely rocky**

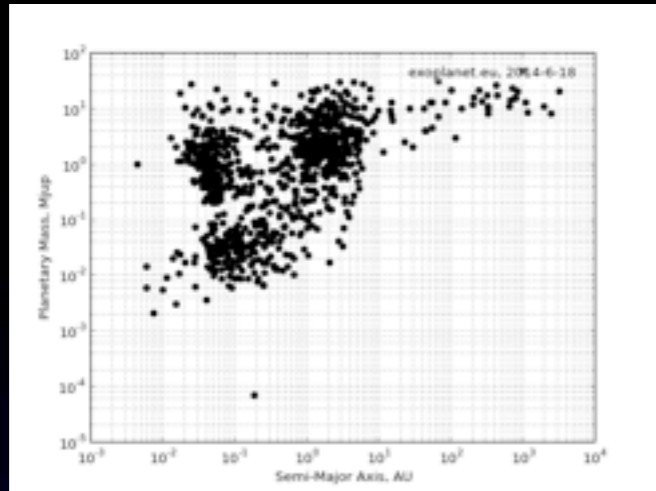
Sub-set of samples from Weiss & Marcy 2014
(mass measurements better than 2-sigma)



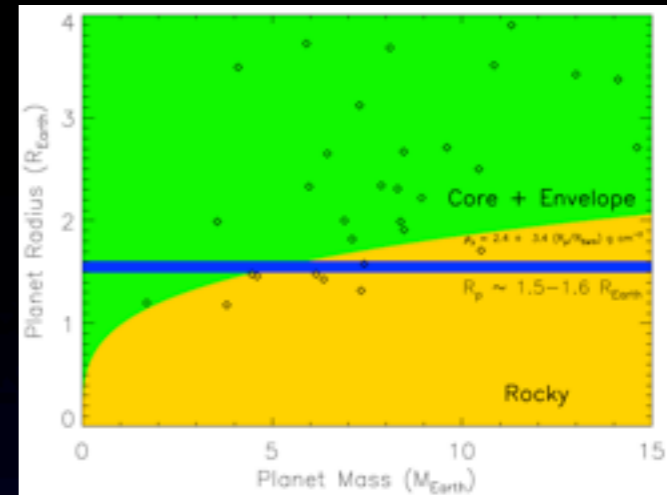
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Derived invaluable constraints on
the formation and evolution of planetary systems



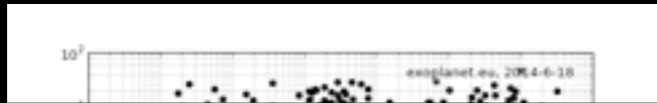
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Derived invaluable constraints on
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Provide a physical explanation, using theoretical models



In reality, it is still difficult...

e.g., Mordasini et al 2012, Ida et al 2013, Hansen & Murray 2013, Chiang & Laughlin 2013

- 1) many processes are involved:
formation, migration, disk evolution, dynamics,
photoevaporative mass loss, & etc...

- 1) unclear formation mechanisms:
a scaled-up version of rocky planet formation
vs
a scaled-down version of gas giant formation

Planet traps + core accretion can simplify
a picture of planet formation in gas disks

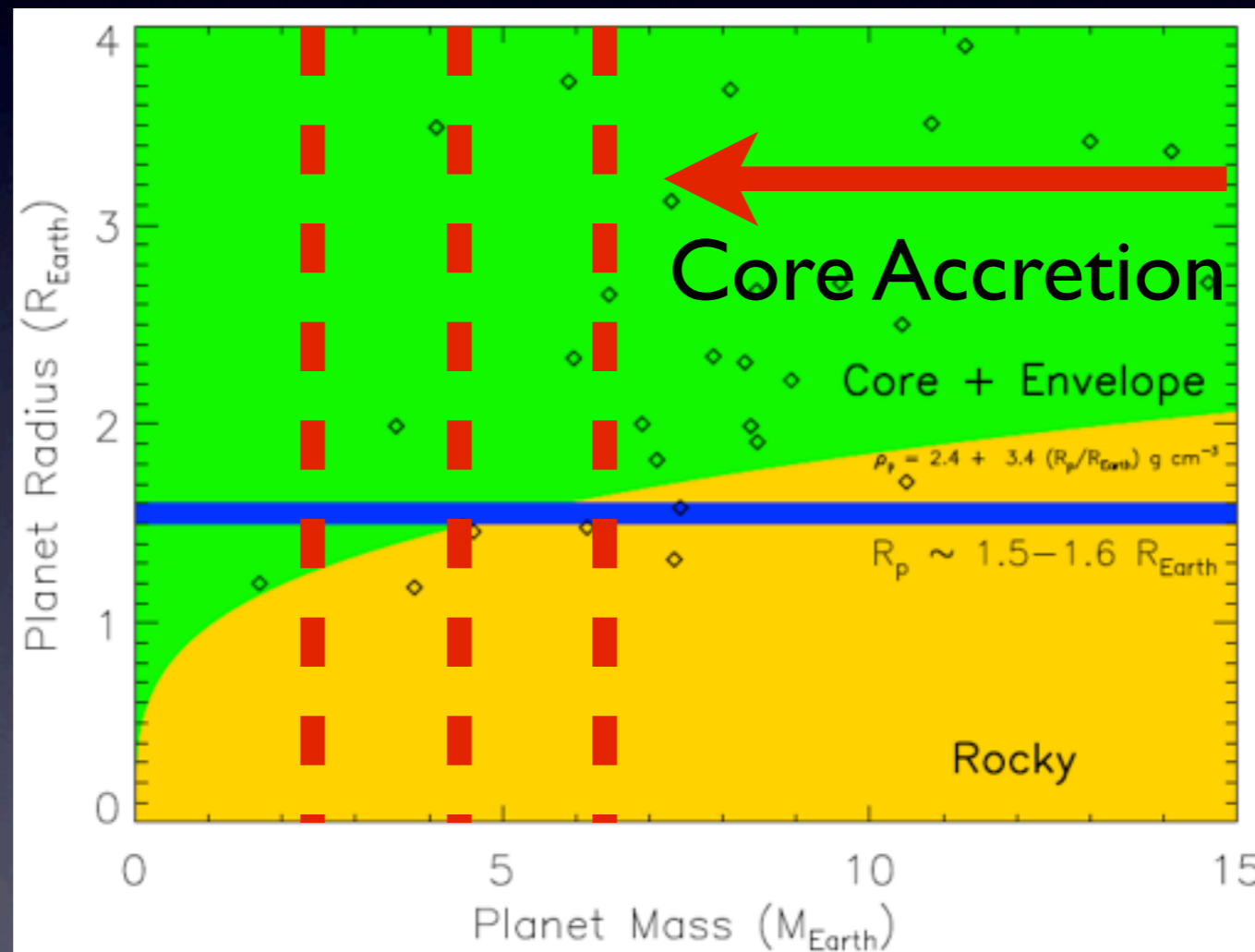
Step 1: planet traps - direct connection with
disk evolution

Step 2: evolutionary tracks of forming planets
at planet traps

Step 3: planet formation frequencies (PFFs) -
our version of population synthesis calculations

Failed Core Scenario:

Planet traps + Core accretion

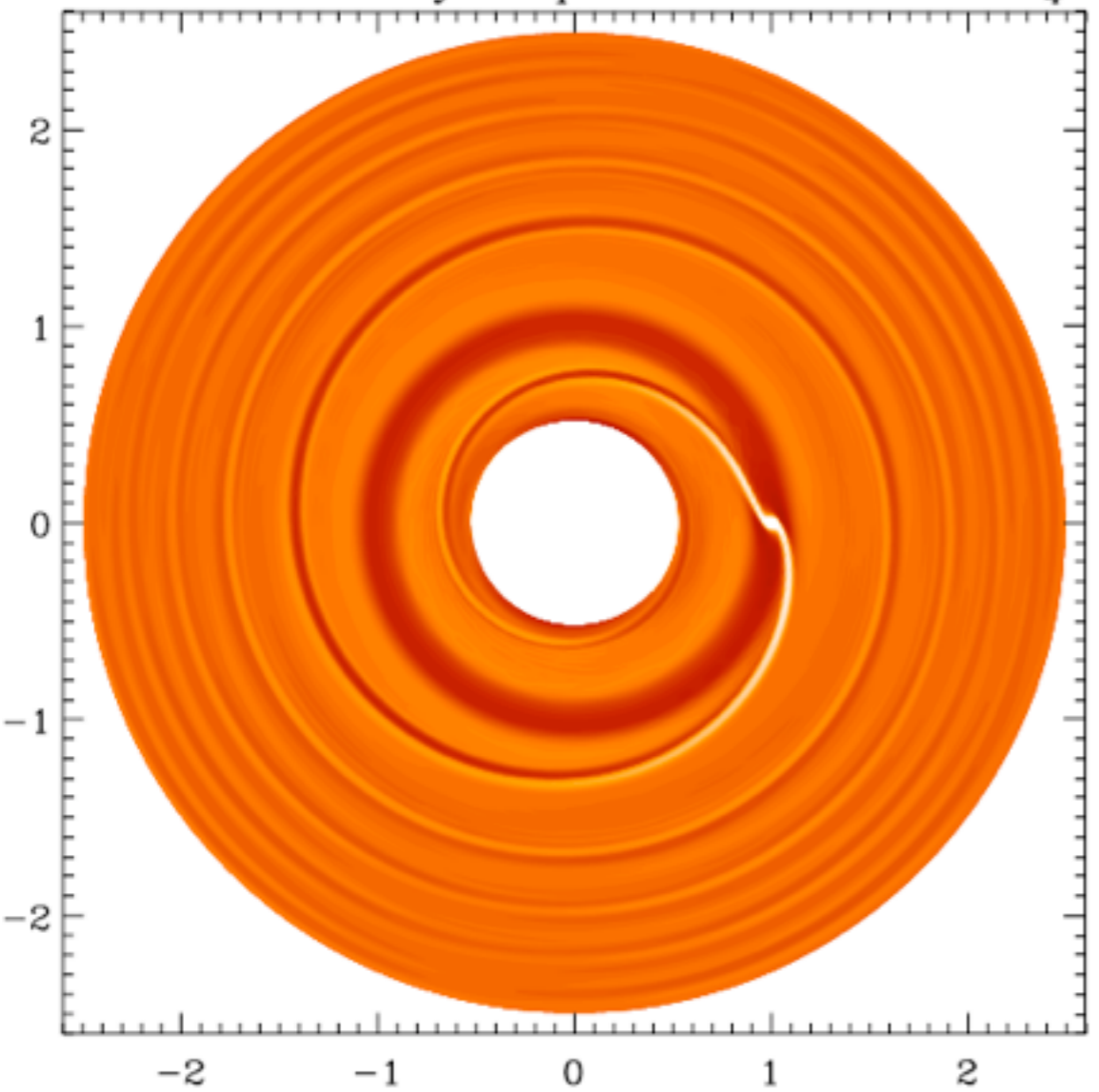


What is the minimum mass of planets formed at planet trap by core accretion??

Step 1: Planet Traps

Step I: Planet Traps

Surface density map at end of run R17₄



Masset 2002

Rapid type I migration

e.g. Goldreich & Tremaine 1980, Ward 1986, 1997, Masset 2001, 2002, Tanaka et al 2002, Baruteau & Masset 2008, Paardekooper et al 2010, 2011, Hasegawa & Pudritz 2011a

Angular momentum transfer

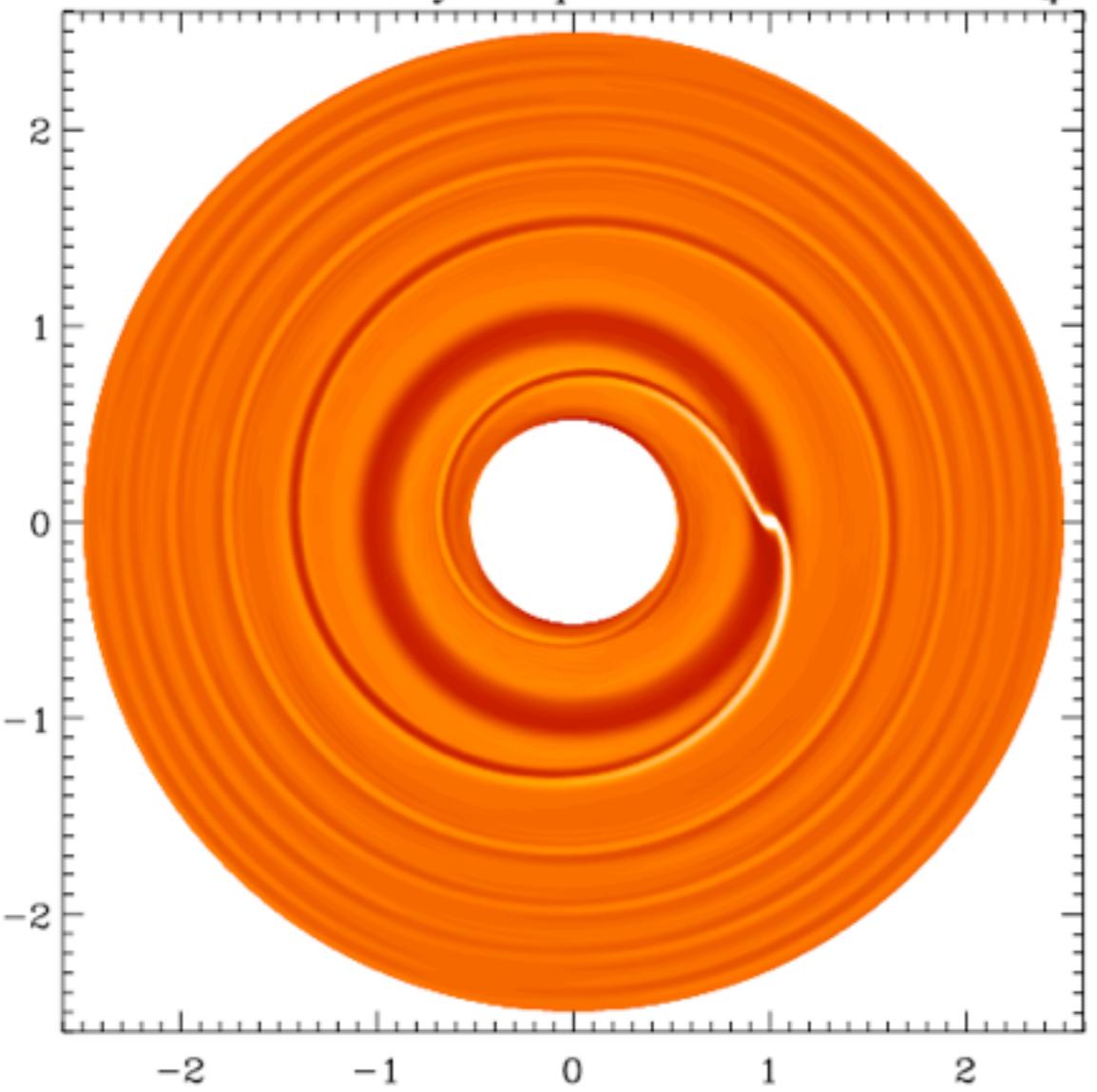
: Lindblad & corotation resonances

The direction of migration

: depends sensitively on disk properties such as the surface density, disk temperature, & opacity

Step I: Planet Traps

Surface density map at end of run R17₄



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Rapid type I migration

e.g. Goldreich & Tremaine 1980, Ward 1986, 1997, Masset 2001, 2002, Tanaka et al 2002, Baruteau & Masset 2008, Paardekooper et al 2010, 2011, Hasegawa & Pudritz 2011a

Angular momentum transfer

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The direction of migration

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Planet traps = disk structures
at which the net tidal torque is zero

Step 1: Planet Traps

Masset et al 2006 **Matsumura, Pudritz, & Thommes 2007, 2009**

Ida & Lin 2008, Morbidelli et al 2008

Hasegawa & Pudritz 2010b, Lyra et al 2010

Hasegawa & Pudritz 2011b, Bitsch & Kley 2011

Hellary & Nelson 2012, Kretke & Lin 2012, Mordasini et al 2012

Pierens et al 2013, Bitsch et al 2013, etc...

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Step 1: Planet Traps

Masset et al 2006 **Matsumura, Pudritz, & Thommes 2007, 2009**

Acceptable conclusion may be...

some kinds of traps are very likely
to be present in protoplanetary
disks

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Step 1: Planet Traps

Hasegawa & Pudritz 2011b

3 types of traps in single disks

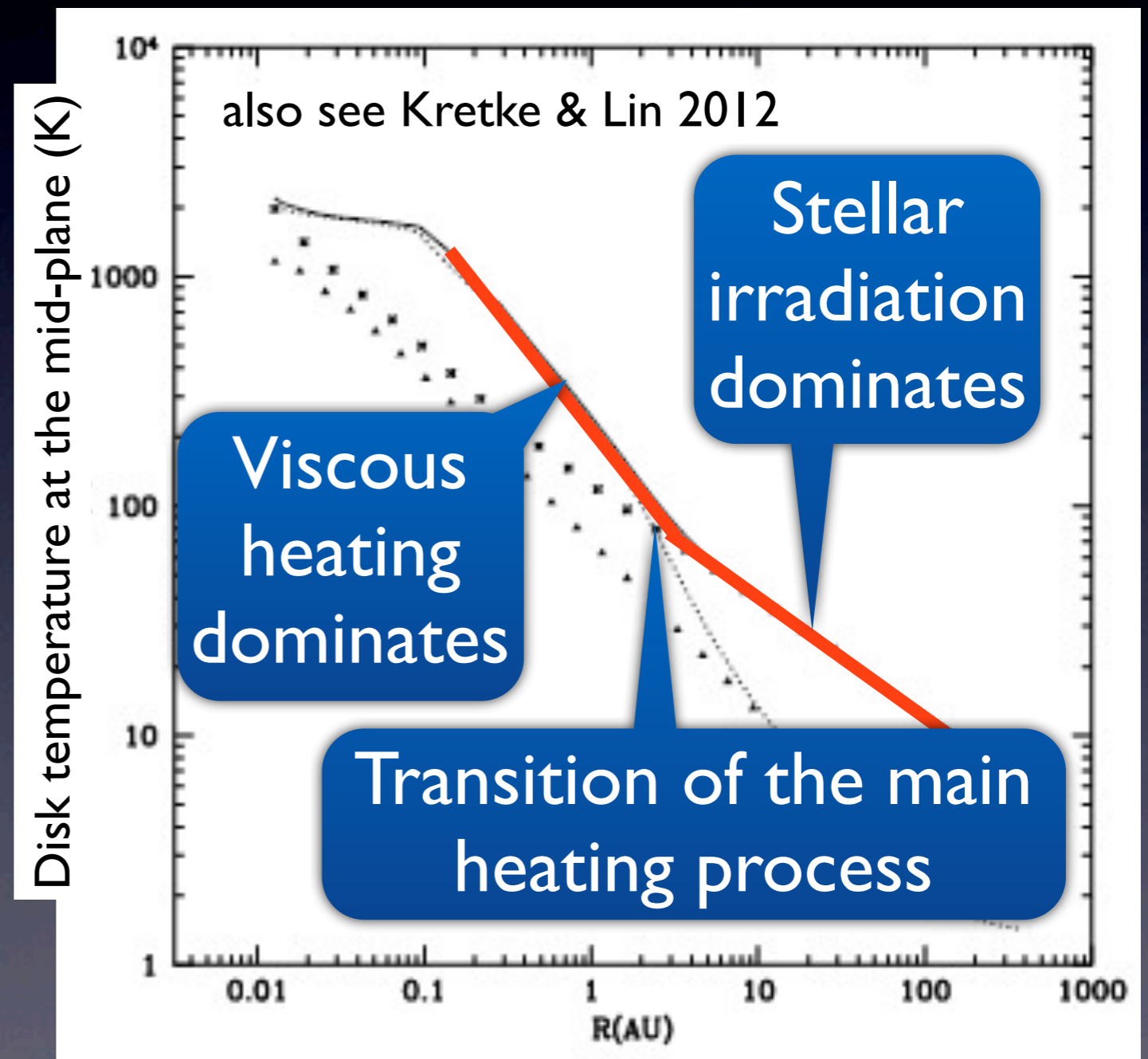
: the outer edge of dead zones, ice lines, heat transitions

Step 1: Planet Traps

Hasegawa & Pudritz 2011b

3 types of traps in single disks

: the outer edge of dead zones, ice lines, **heat transitions**



D'Alessio et al 1998

Step 1: Planet Traps

Hasegawa & Pudritz 2011b

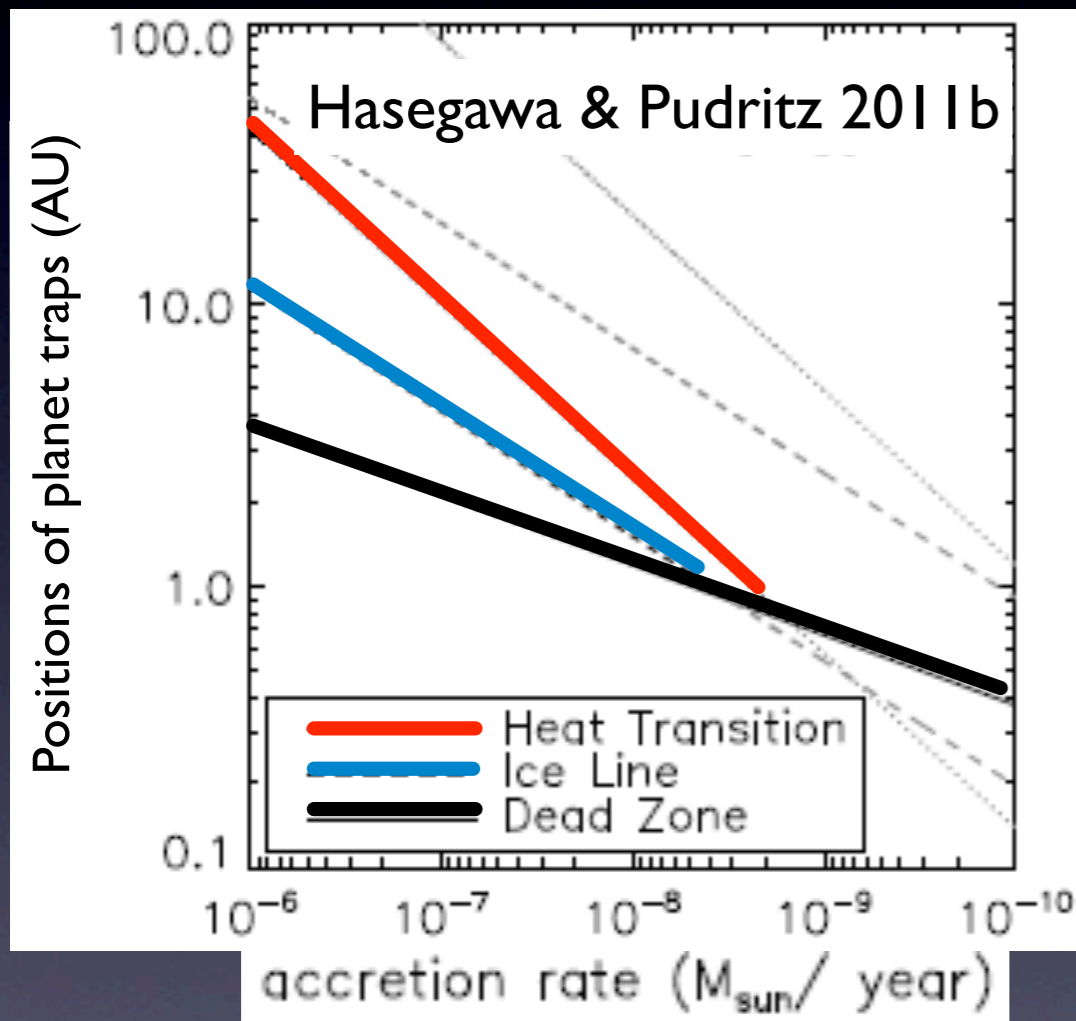
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Step 1: Planet Traps

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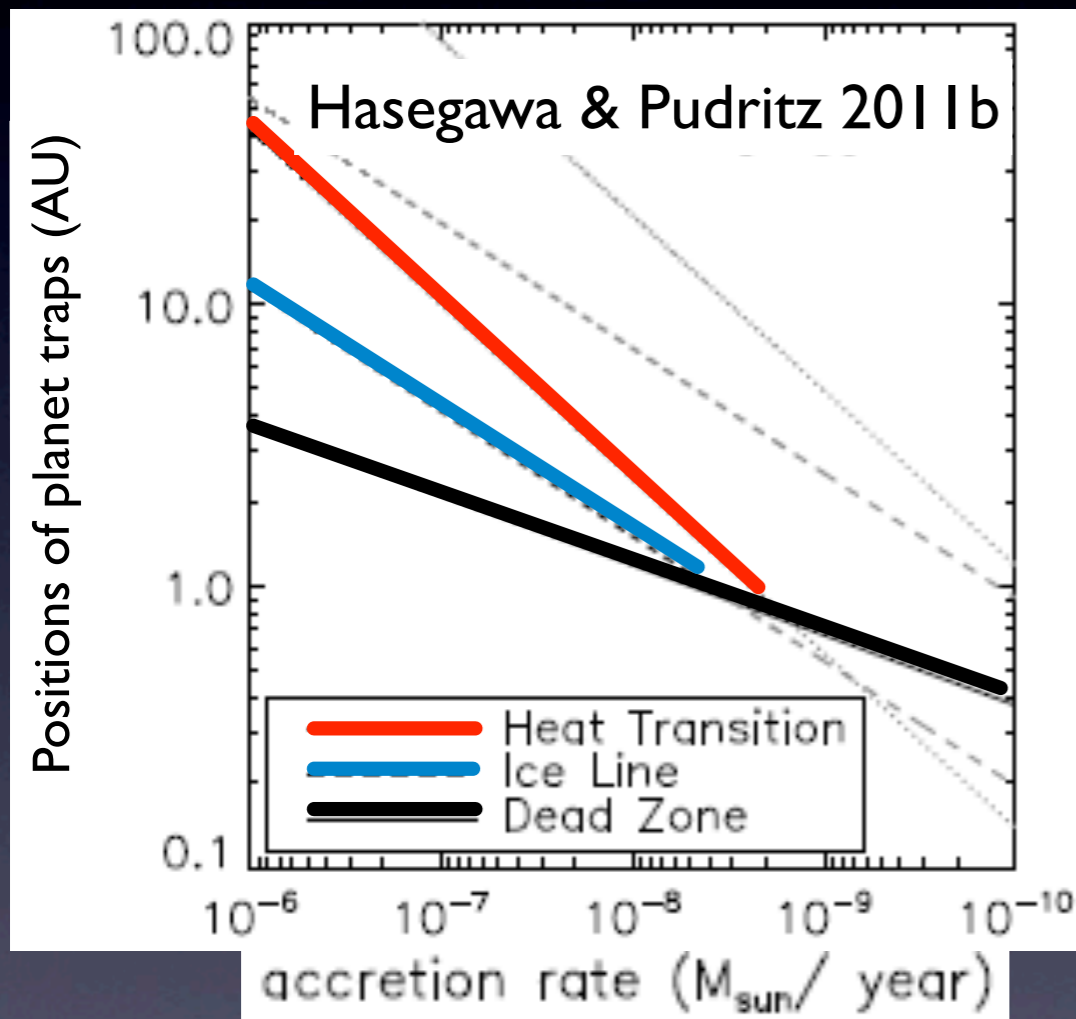


Locations of traps are specified by disk evolution

Step 1: Planet Traps

3 types of traps in single disks

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Locations of traps are specified by disk evolution

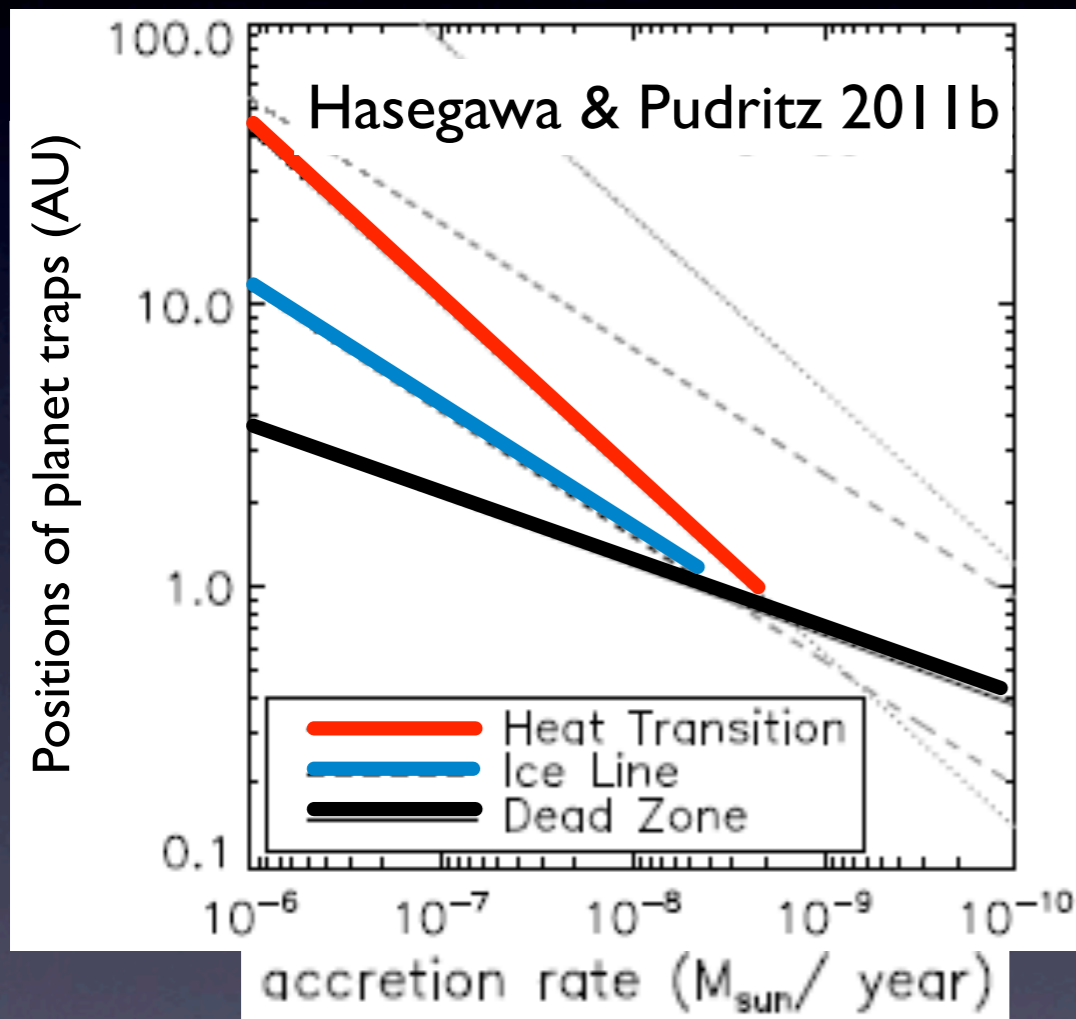
Mass dependence of traps

: planet traps are effective until protoplanets obtain the gap-opening mass & undergo type II migration

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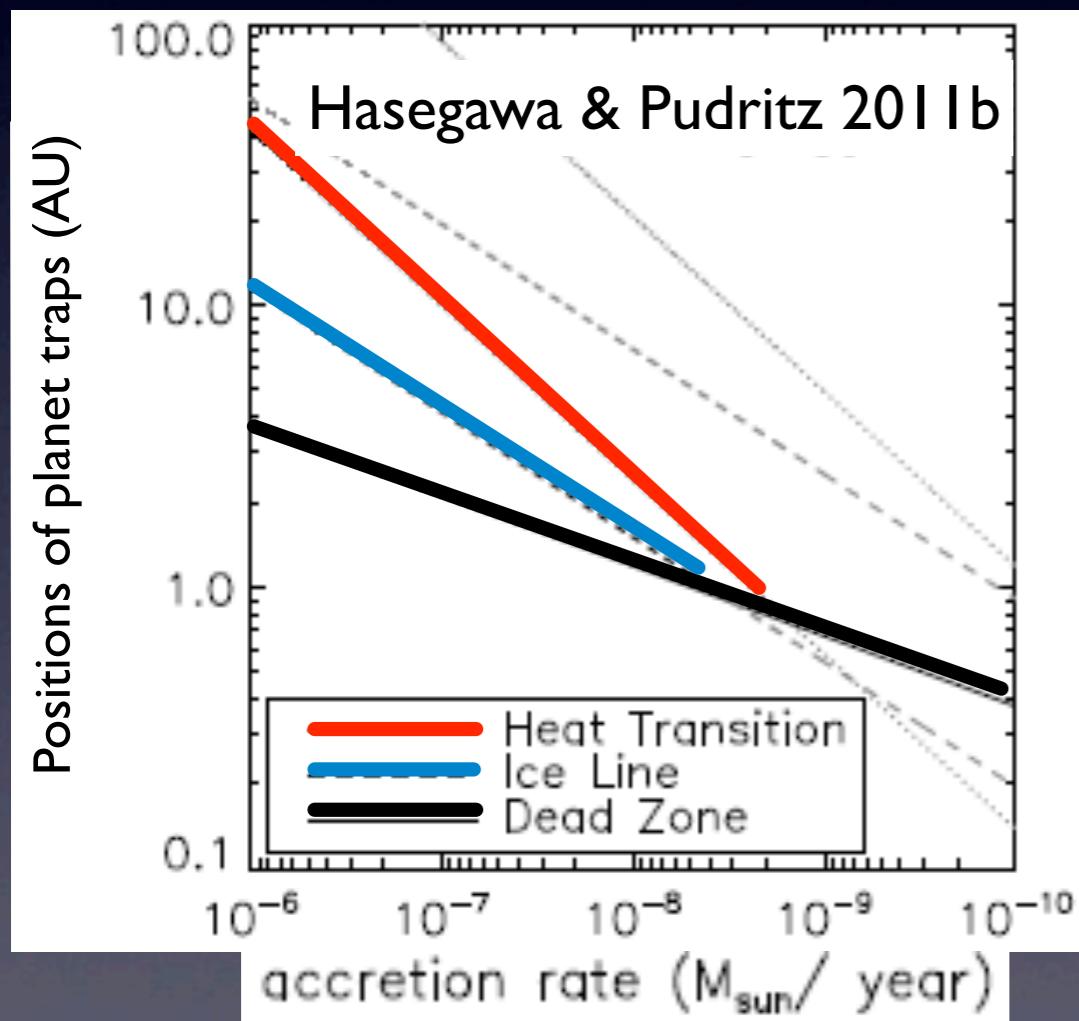
Mass dependence of traps

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Planets form locally at traps before type II migration

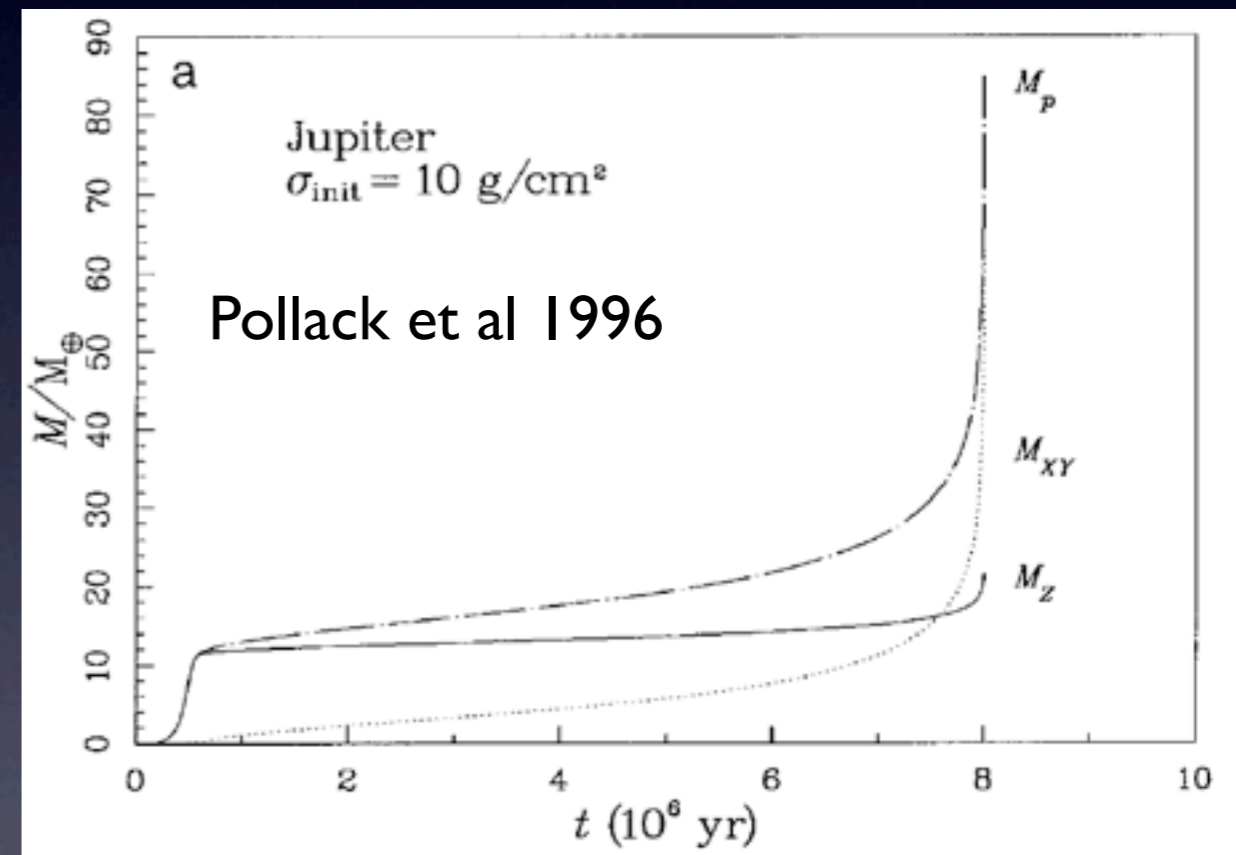
Step 2: Evolutionary Tracks

Planet traps



+

Core accretion



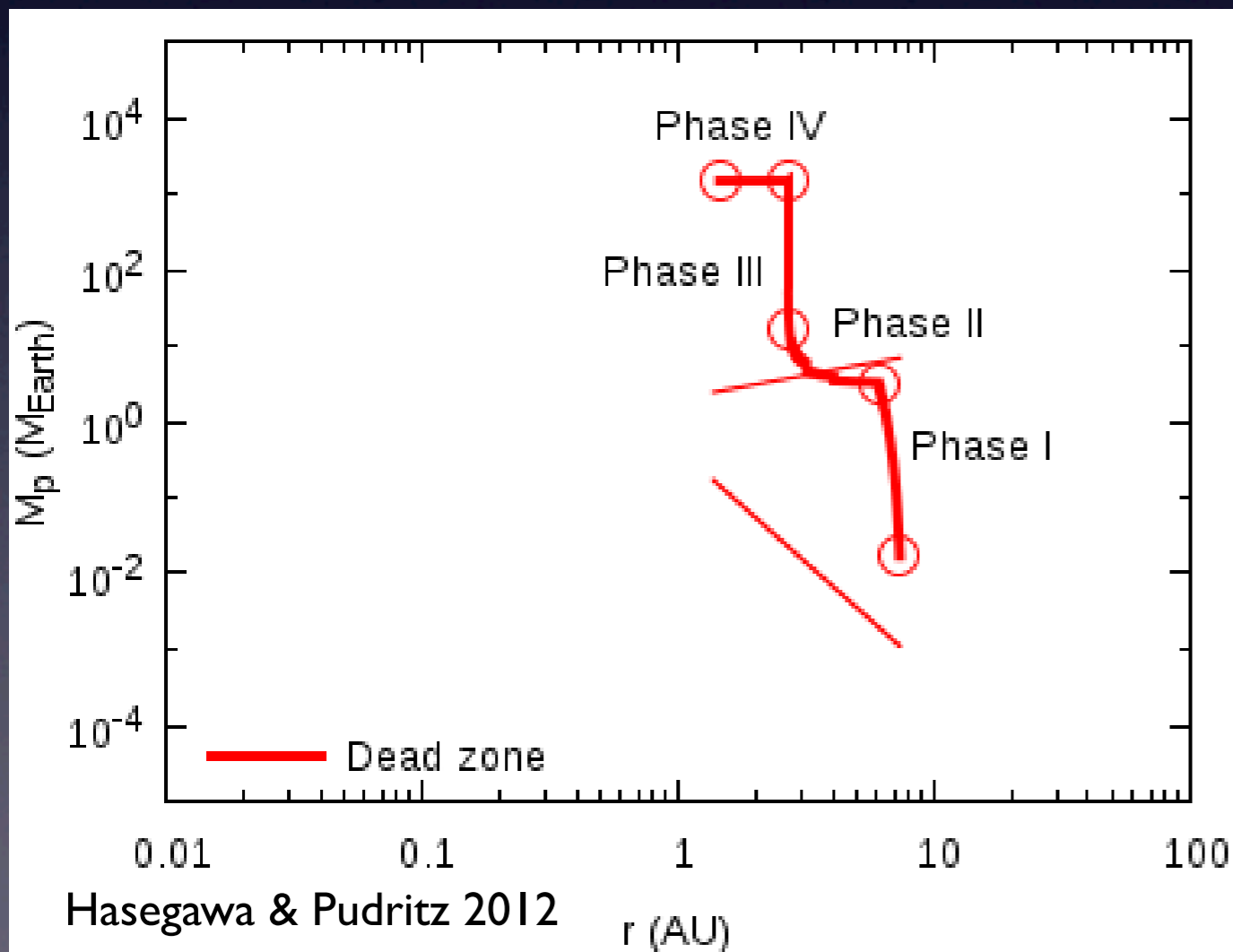
Step 2: Evolutionary Tracks

Hasegawa & Pudritz 2012

A disk around a classical
T Tauri star is considered

$$M_{disk} \sim 0.03M_{\odot}$$

$$\tau_{disk} \sim 8.8 \times 10^6 \text{ years}$$



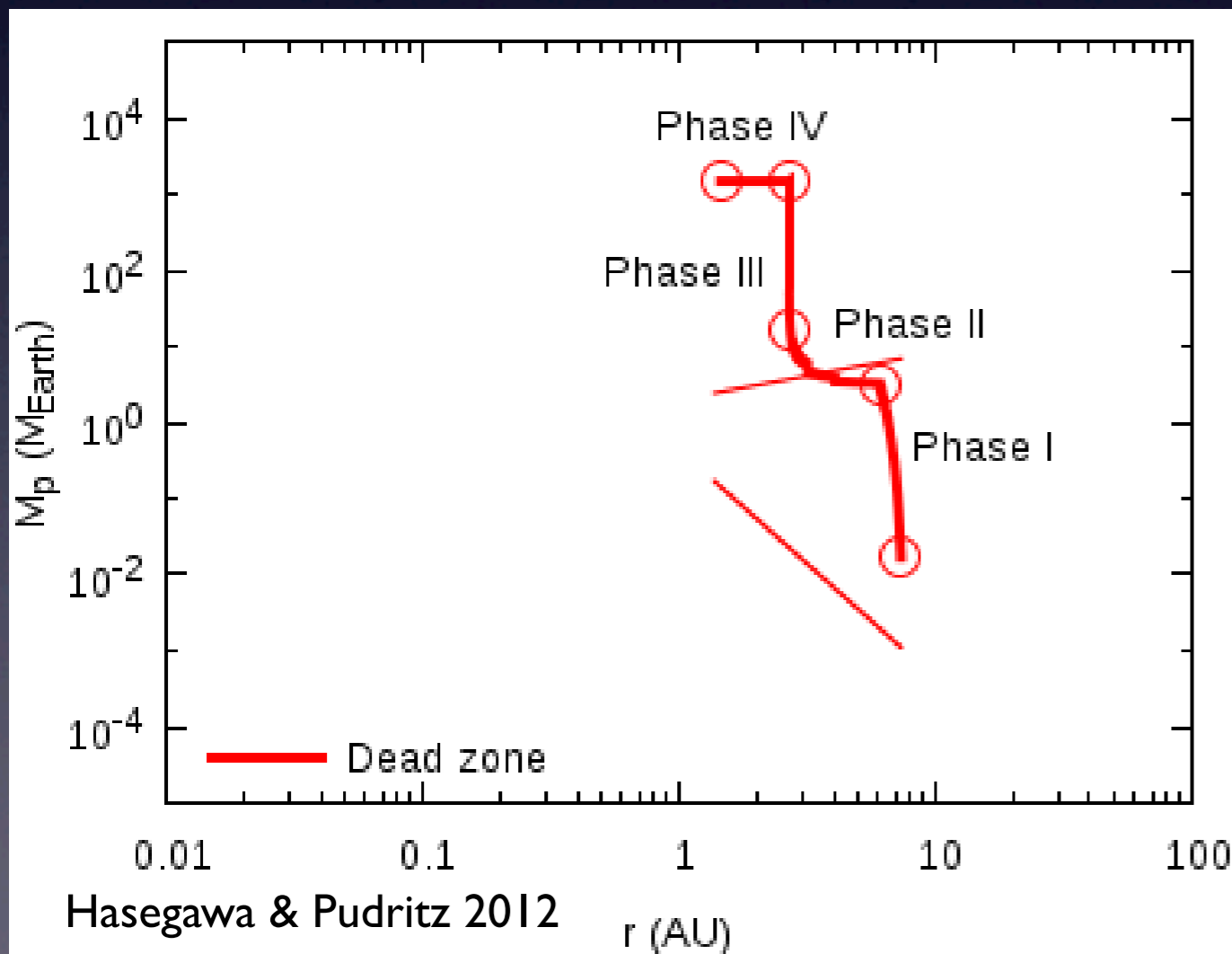
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Gas disks totally dissipate

↑ **Phase IV** ($> 10^6 \text{ years}$)

Gas giants

↑ **Phase III** ($< 10^5 \text{ years}$)

Cores + low-mass atmospheres

↑ **Phase II**
($\sim 2 \times 10^6 \text{ years}$)

Cores of gas giants

↑ **Phase I** ($< 10^6 \text{ years}$)

Dust/Planetesimals

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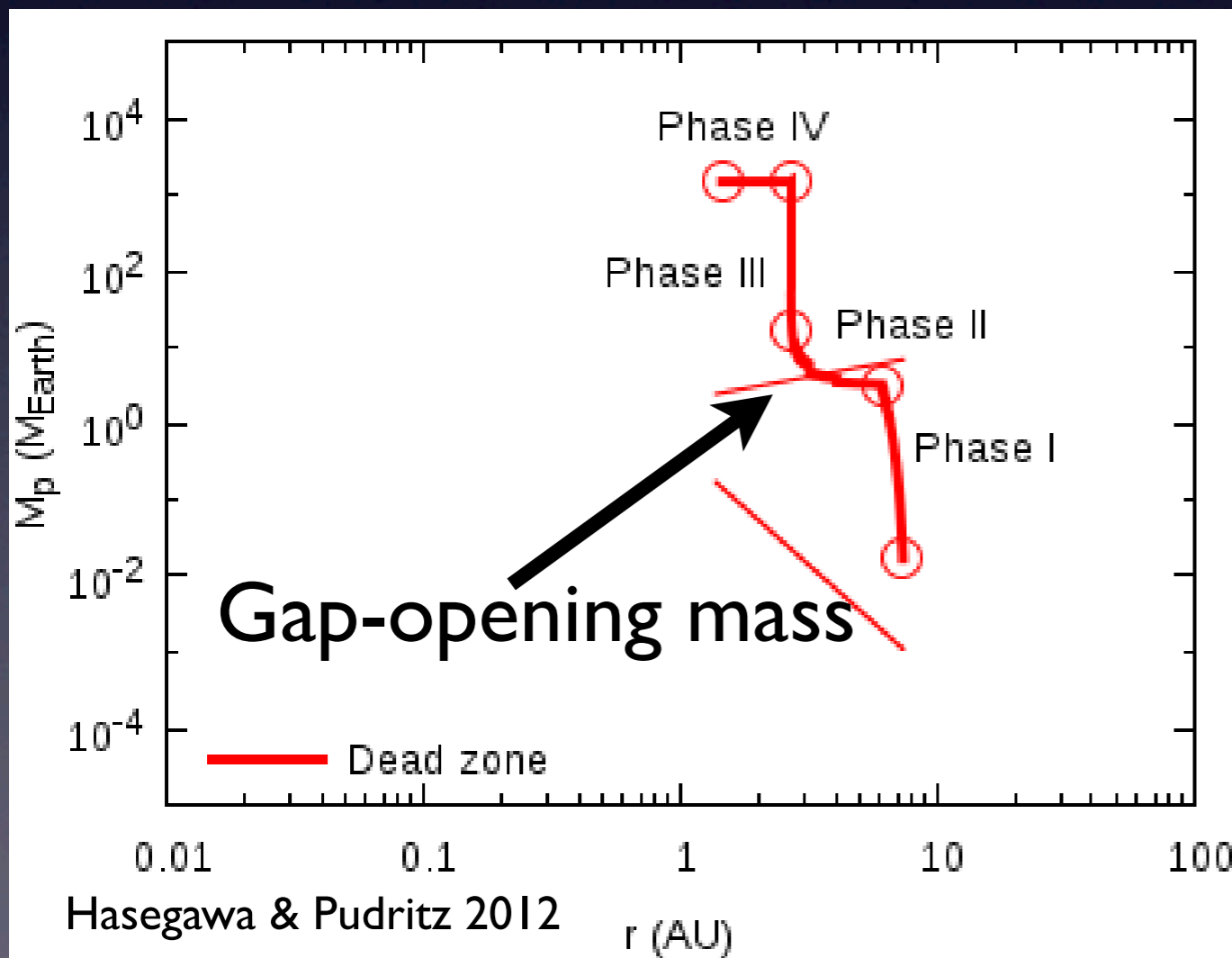
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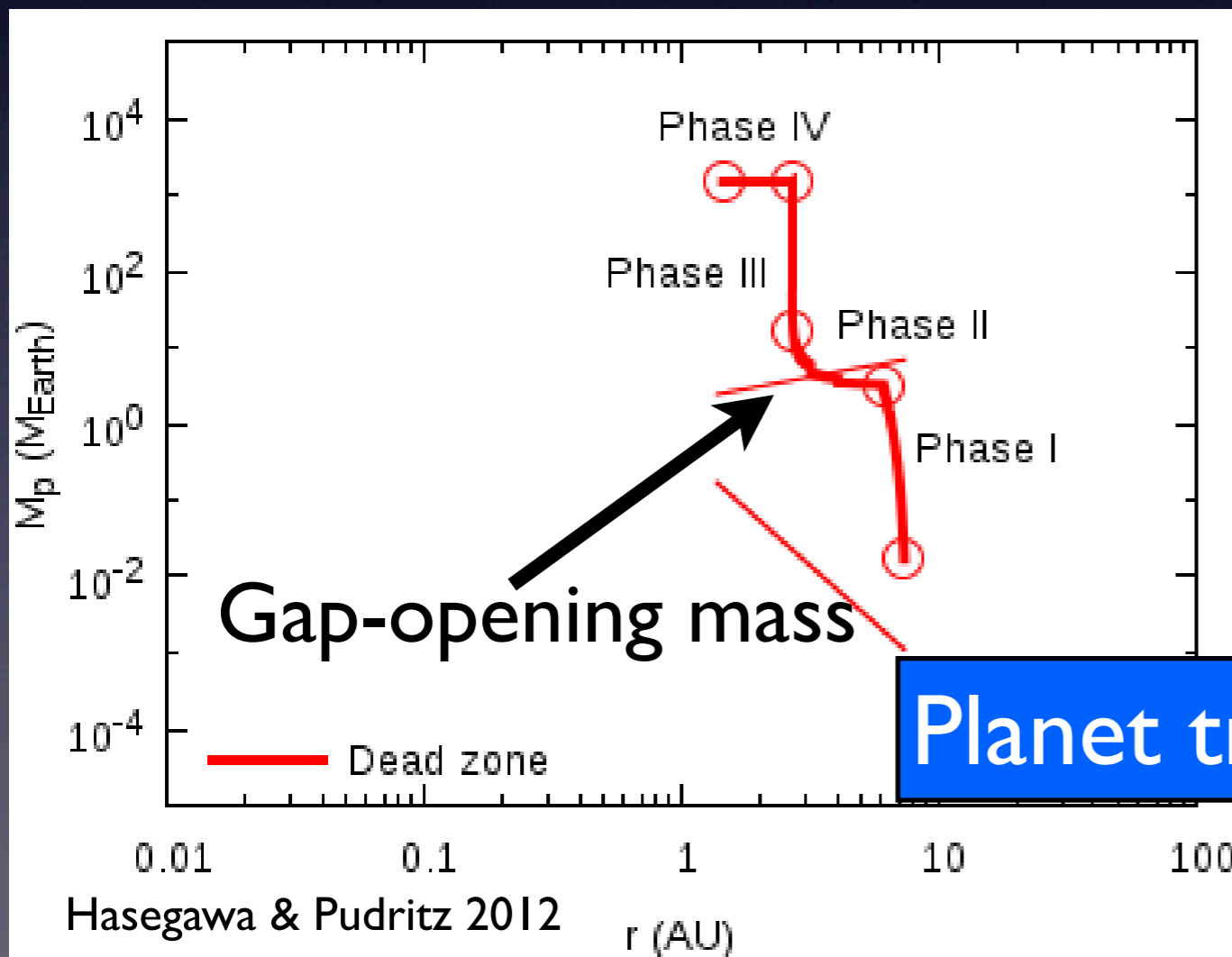
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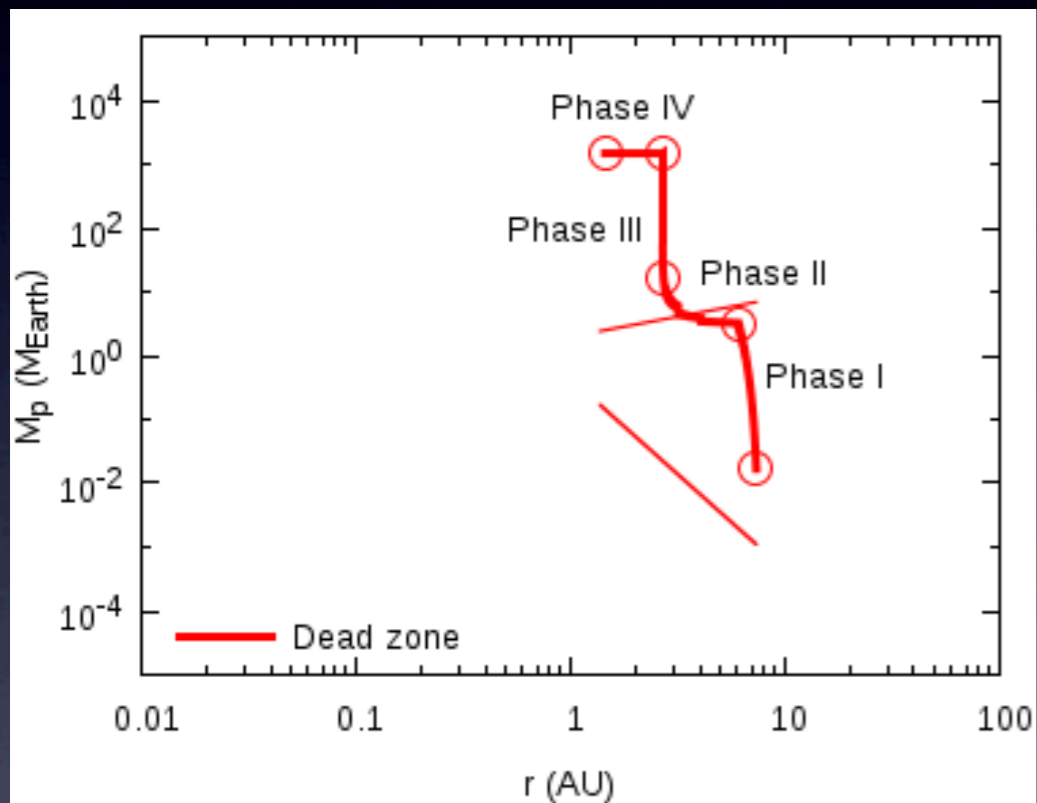
Cores of gas giants

Phase I ($< 10^6 \text{ years}$)

Dust/Planetesimals

Step 3: Statistics

Hasegawa & Pudritz 2013



Statistical
quantities

Step 3: Statistics

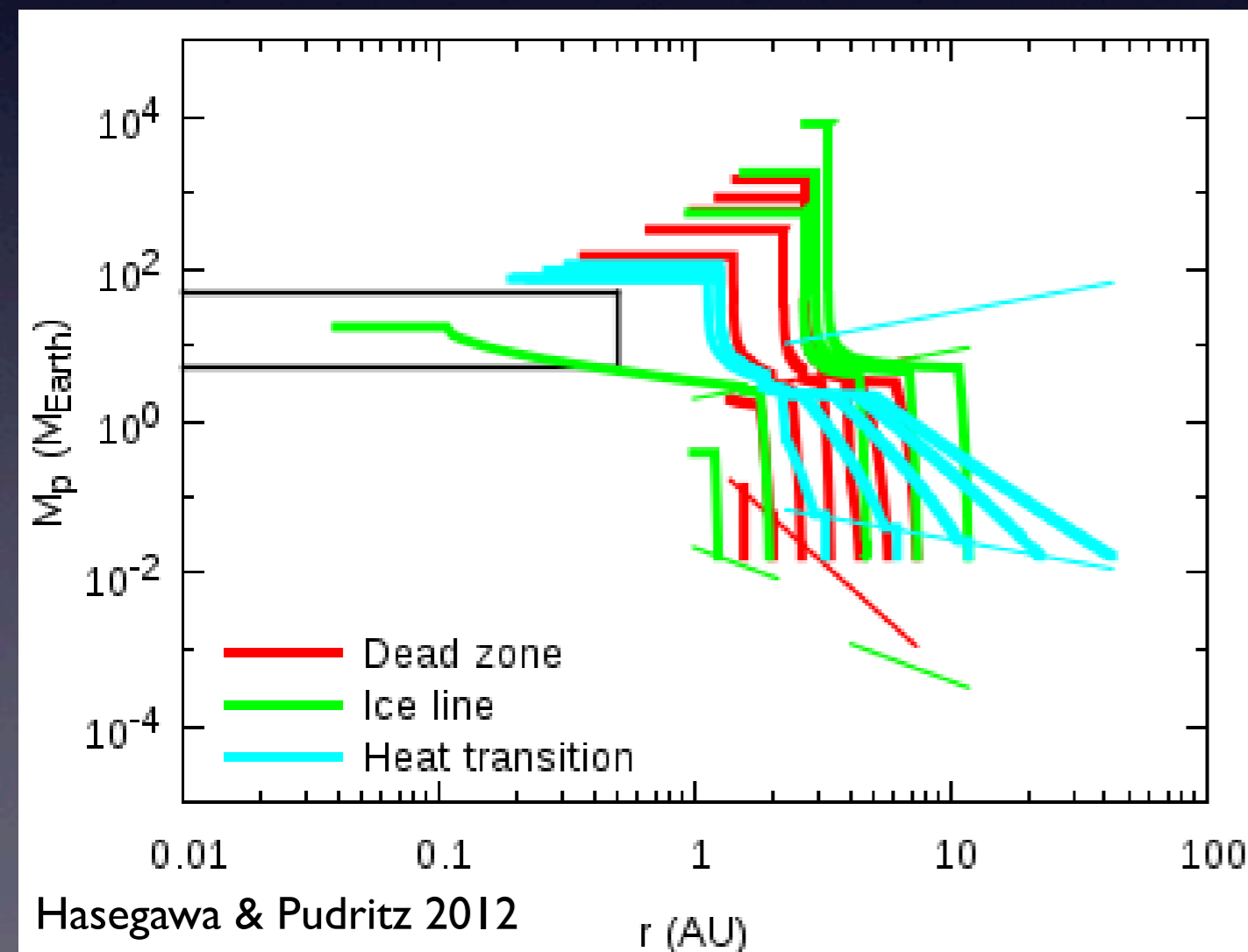
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Compute lots of tracks

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Step 3: Statistics

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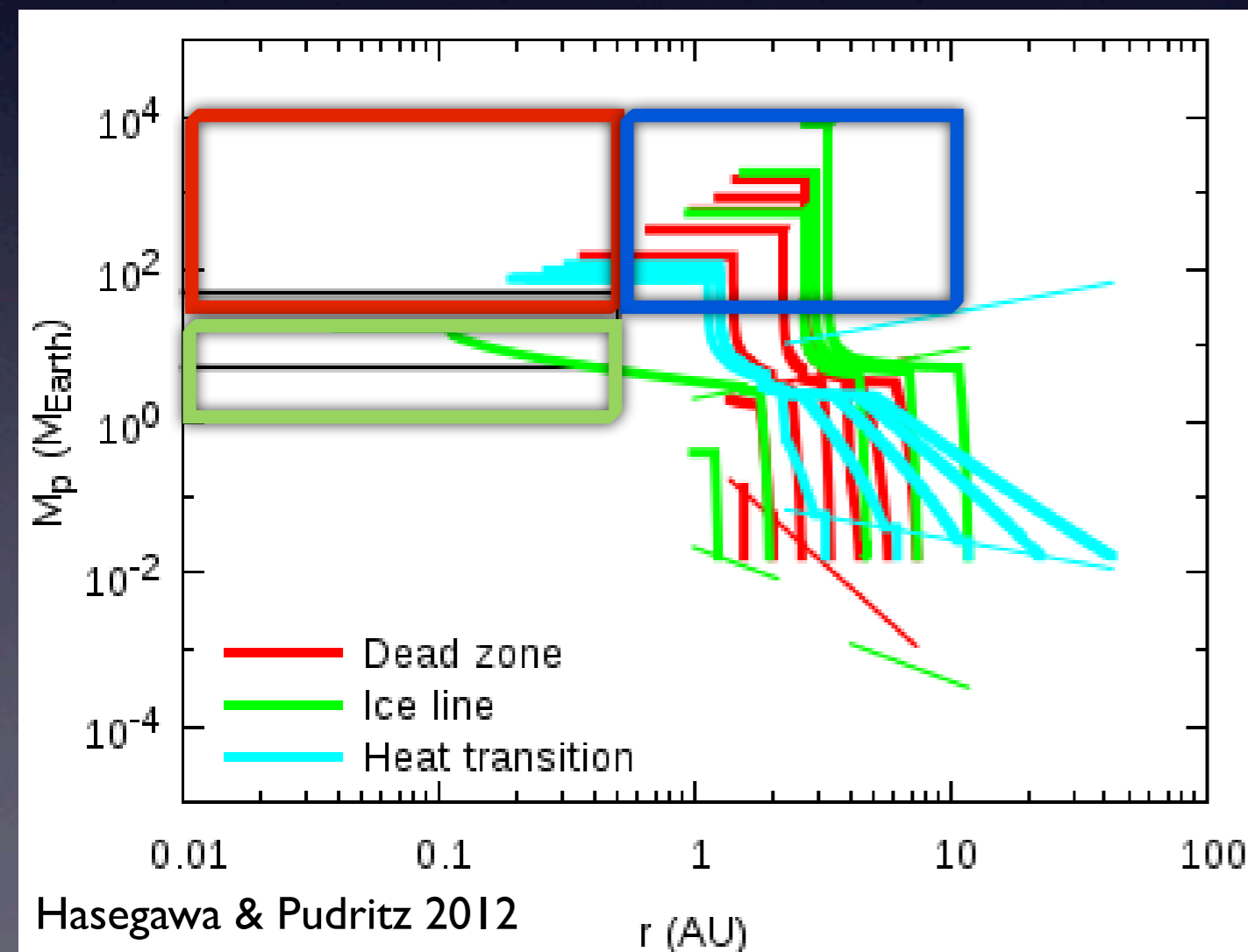
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Partition the diagram



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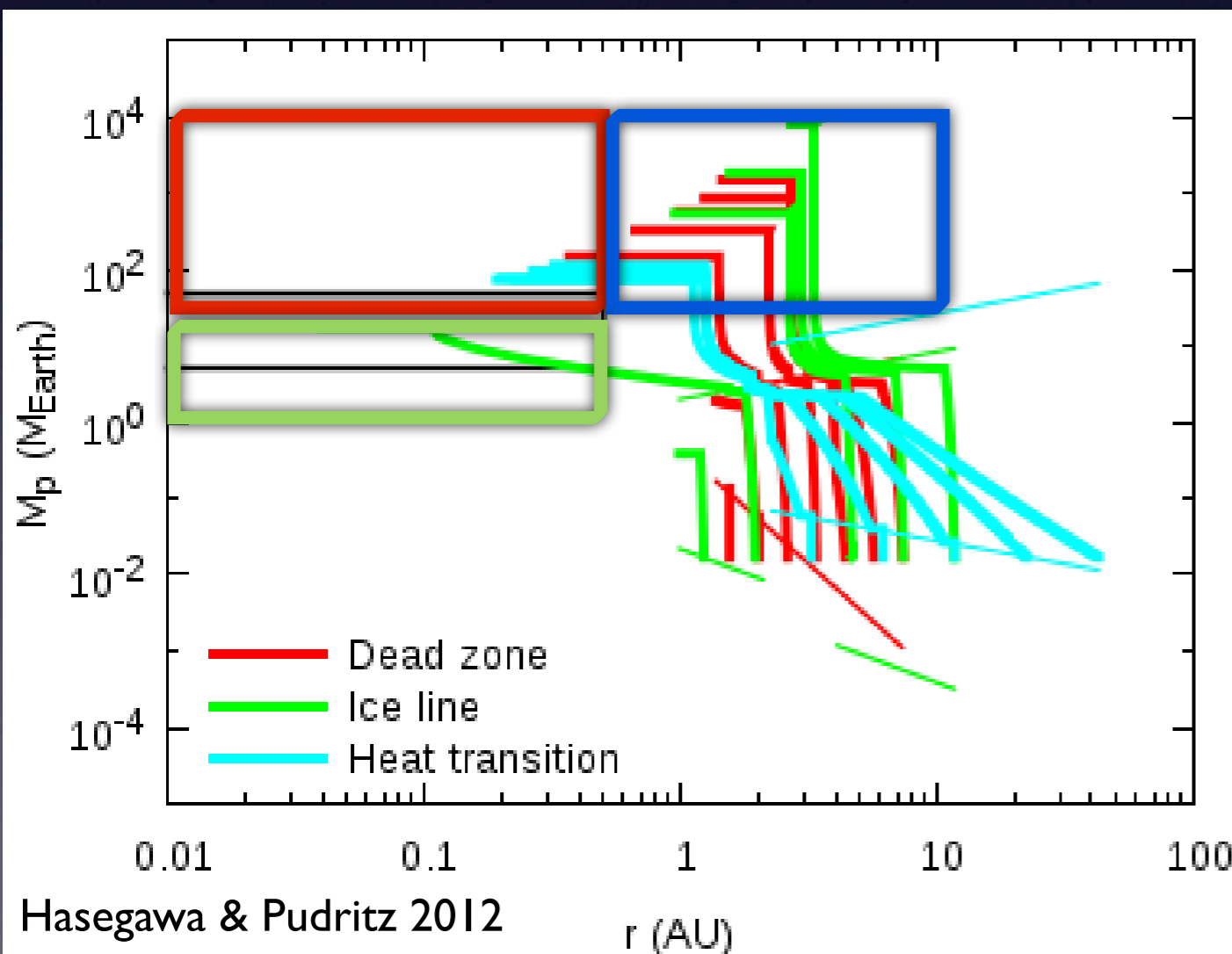
Calculate planet formation frequencies (PFFs)

$$PFFs \equiv \sum_{\eta_{acc}} \sum_{\eta_{dep}} \frac{N(\eta_{acc}, \eta_{dep})}{N_{int}}$$

$$\times w_{mass}(\eta_{acc}) w_{lifetime}(\eta_{dep})$$



Weight functions related to disk observations



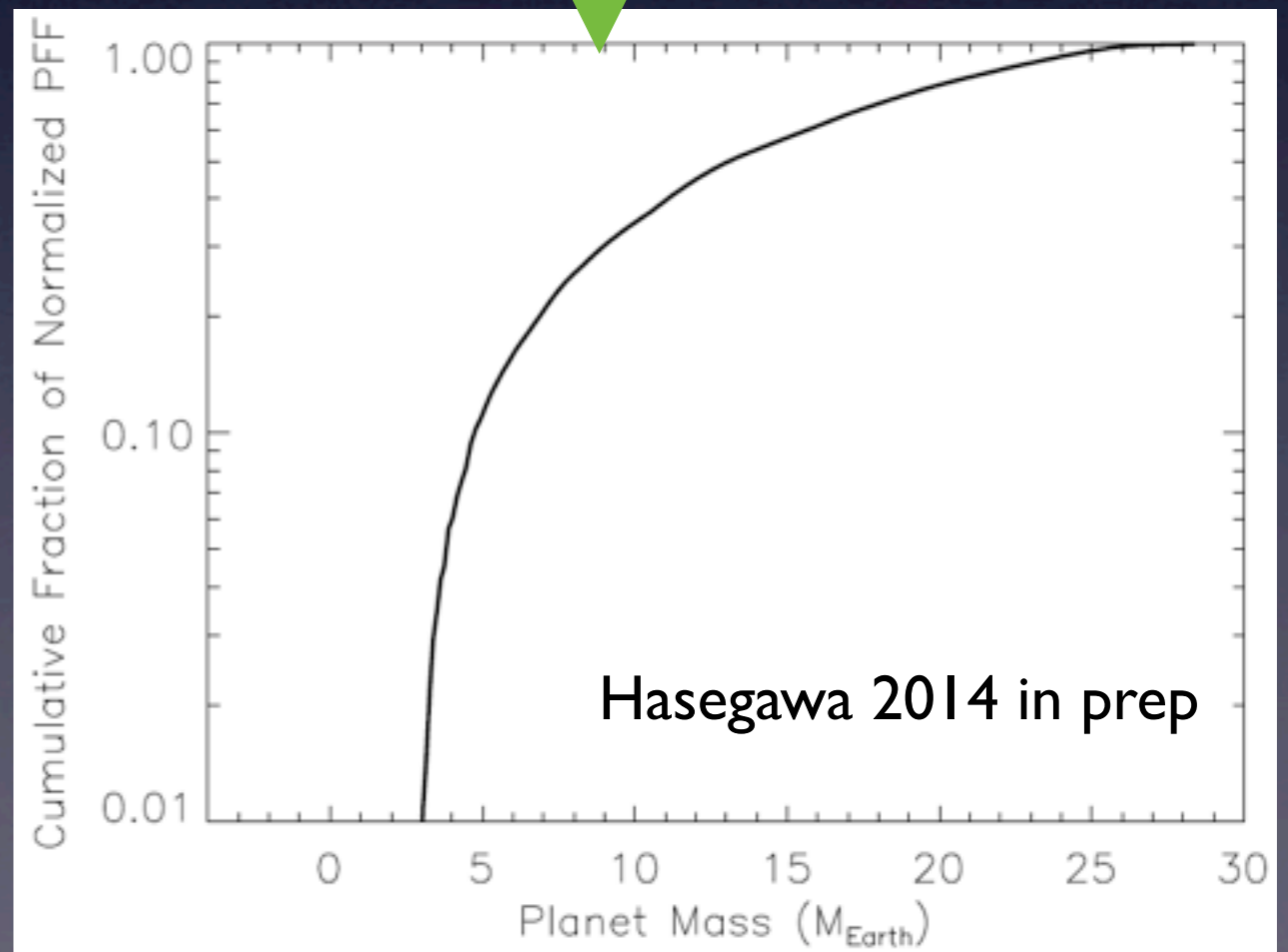
$1M_{\odot}$	Hot Jupiters	Exo-Jupiters	Super-Earths	Total
PFF				

$1M_{\odot}$	Hot Jupiters	Exo-Jupiters	Super-Earths	Total
PFF	~ 7.6 %	~ 25.3 %	~ 10.2 %	43.1%

A considerable fraction of observed super-Earths may be formed as failed cores of gas giants (mini-gas giants)

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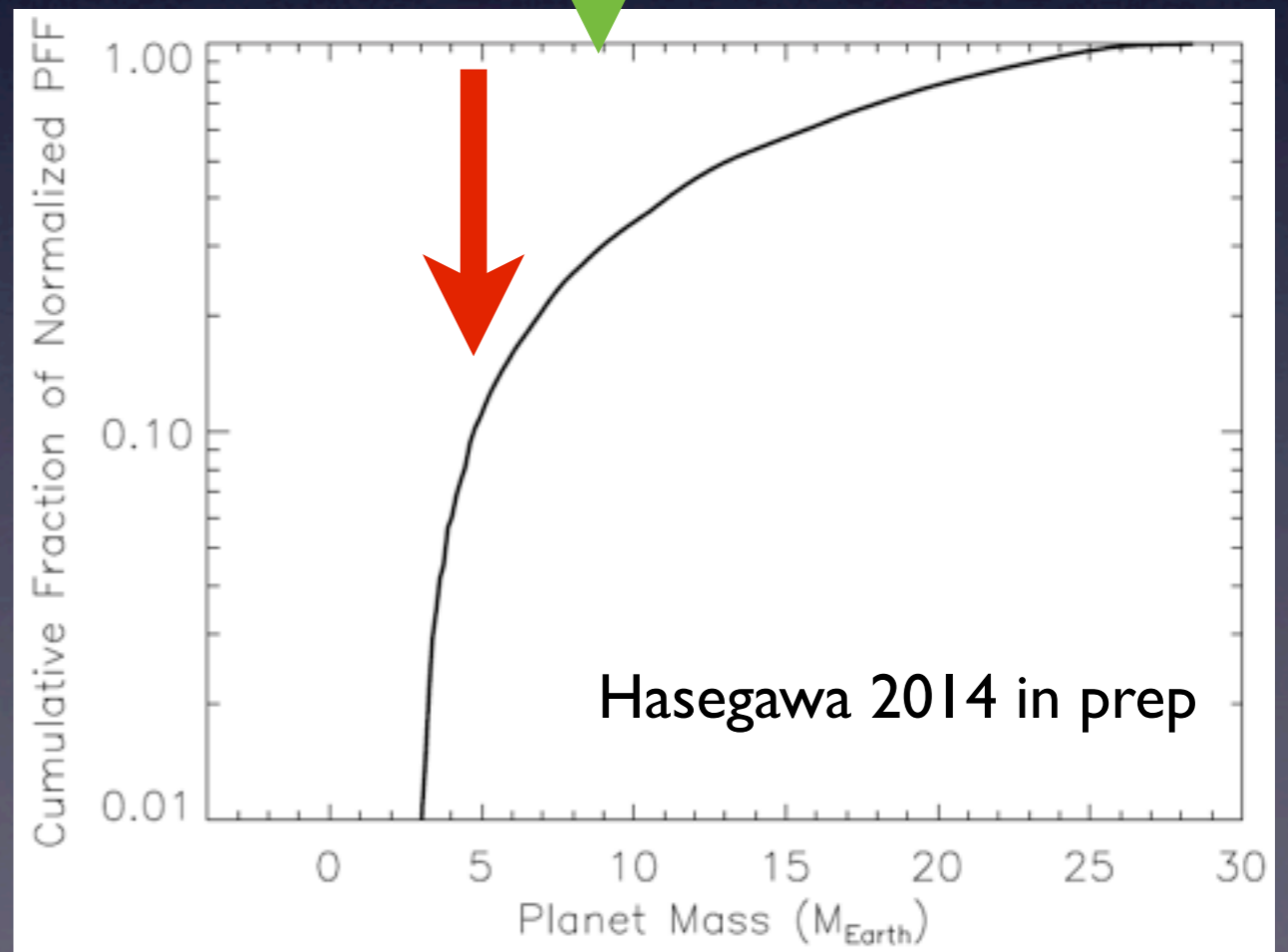


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A considerable fraction of observed super-Earths may be formed as failed cores of gas giants (mini-gas giants)

The minimum mass of planets formed by core accretion at planet traps:

$$M_{min}^{CA} \simeq 4 - 5M_{\oplus}$$



Why $M_{min}^{CA} \simeq 4 - 5 M_{\oplus}$??

Hasegawa 2014 in prep

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1) photoevaporative mass loss of planets

Why $M_{min}^{CA} \simeq 4 - 5M_{\oplus}$??

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1) photoevaporative mass loss of planets

=> No, for our model, since it is NOT included yet

Why $M_{min}^{CA} \simeq 4 - 5M_{\oplus}$??

Hasegawa 2014 in prep

- 1) photoevaporative mass loss of planets
- 2) the critical core mass to start gas accretion

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Super-Earths

Gas giants

Phase III ($< 10^5 years$)

Cores + low-mass atmospheres

Phase II

($\sim 2 \times 10^6 years$)

Cores of gas giants

Phase I ($< 10^6 years$)

Dust/Planetesimals



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Super-Earths

Gas giants

$$M_c > M_{c,crit} \left(\frac{\dot{M}_c}{10^{-6} M_{\oplus} \text{yr}^{-1}} \right)^{1/4}$$

$M_{c,crit}$: Parameter

$\sim 10M_{\oplus}$ for the canonical case

$< 10M_{\oplus}$ when dust grains grow in atmospheres

Phase III ($< 10^5 \text{ years}$)
Cores + low-mass atmospheres

Phase II
($\sim 2 \times 10^6 \text{ years}$)
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Why $M_{min}^{CA} \simeq 4 - 5M_{\oplus}$??

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1) photoevaporative mass loss of planets

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$M_{c,crit}$	$3M_{\oplus}$	$5M_{\oplus}$	$10M_{\oplus}$
M_{min}^{CA}			

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Hasegawa 2014 in prep

1) photoevaporative mass loss of planets

2) the critical core mass to start gas accretion

$M_{c,crit}$	$3M_{\oplus}$	$5M_{\oplus}$	$10M_{\oplus}$
M_{min}^{CA}	$3.9M_{\oplus}$	$5M_{\oplus}$	$4.6M_{\oplus}$

=> No, M_{min}^{CA} is very insensitive to the critical core mass

Why $M_{min}^{CA} \simeq 4 - 5M_{\oplus}$??

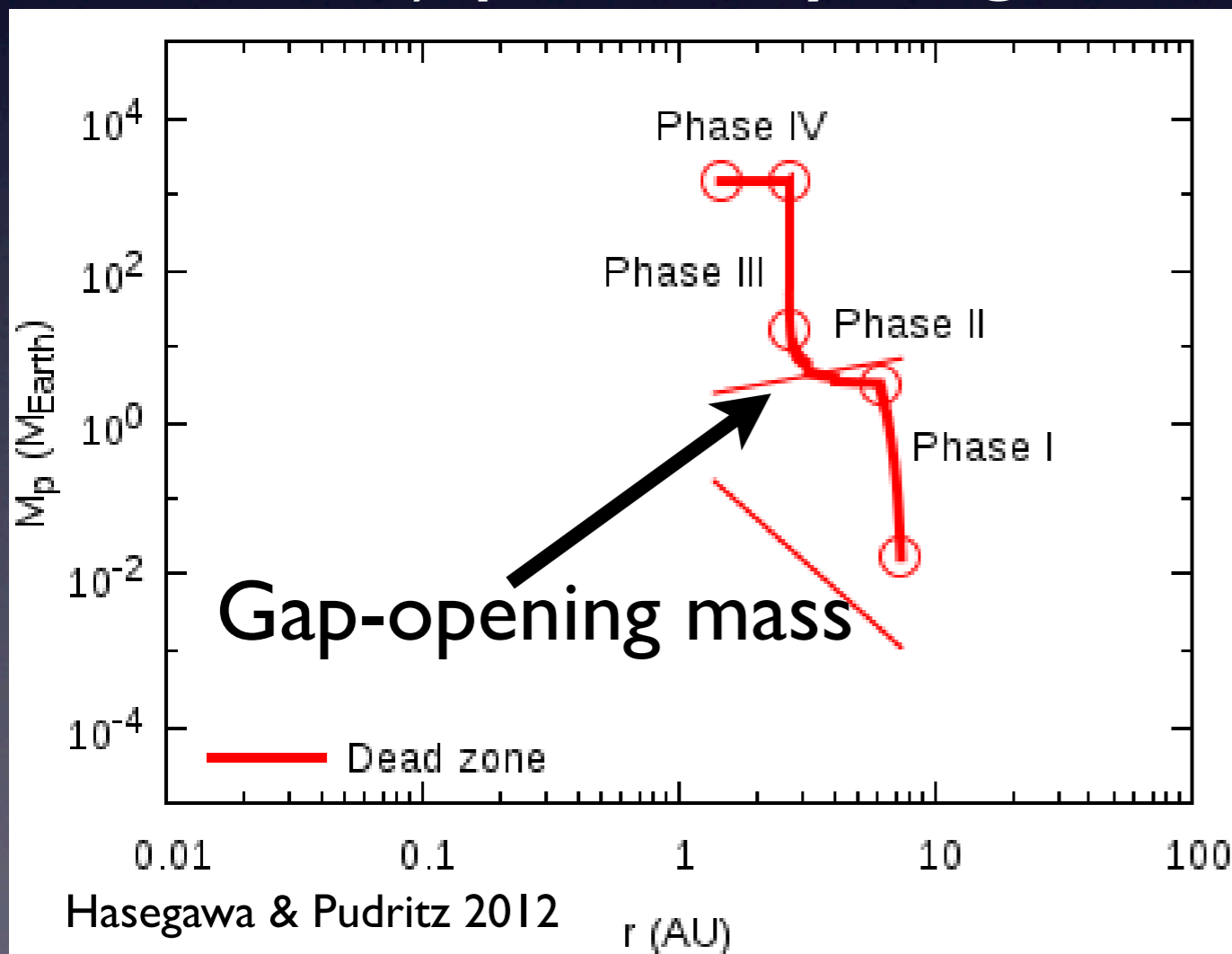
Hasegawa 2014 in prep

- 1) photoevaporative mass loss of planets
- 2) the critical core mass to start gas accretion
- 3) planetary migration in gas disks

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Hasegawa 2014 in prep

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Two kinds of migration
in our model

Planet traps

: transport forming cores
from large radii to > 1 AU

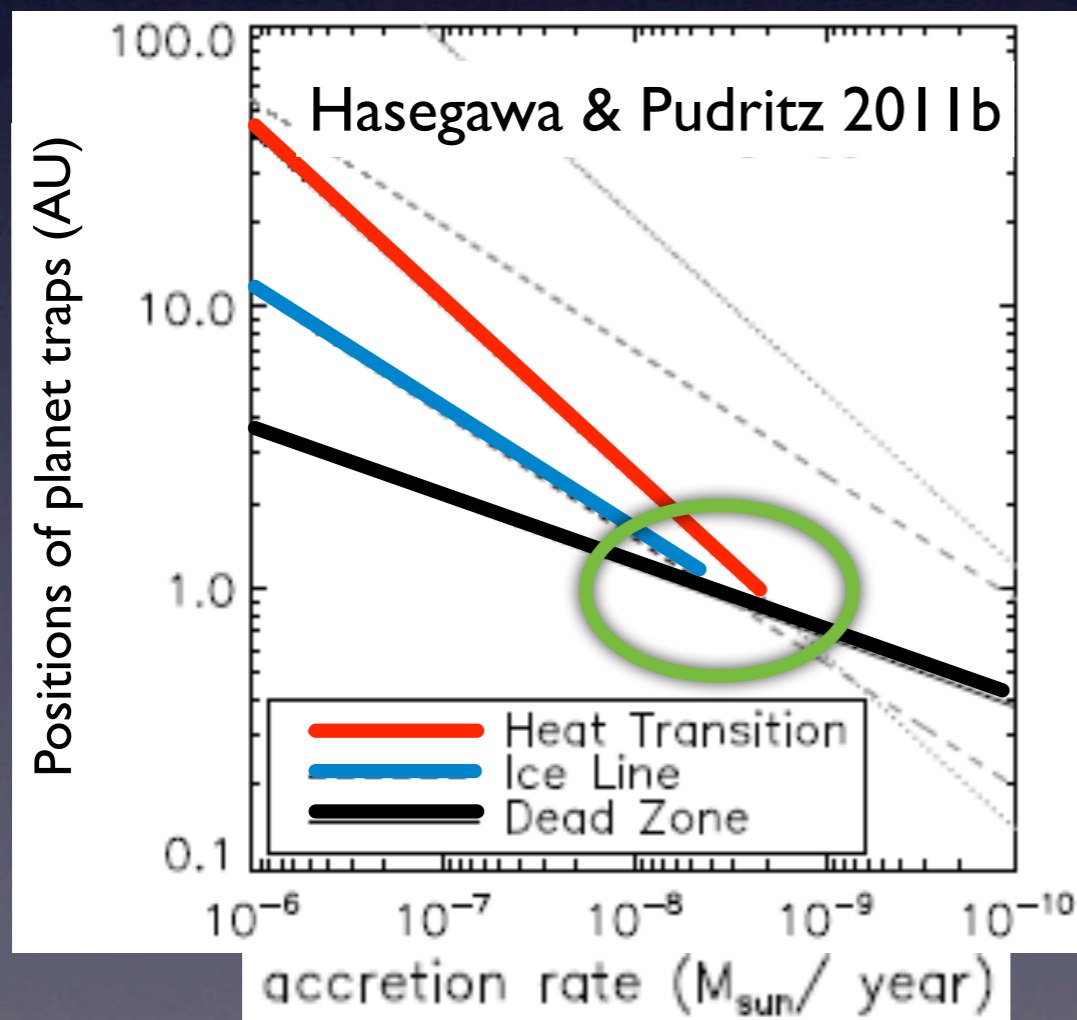
Type II migration

: transport cores with atmospheres
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Hasegawa 2014 in prep

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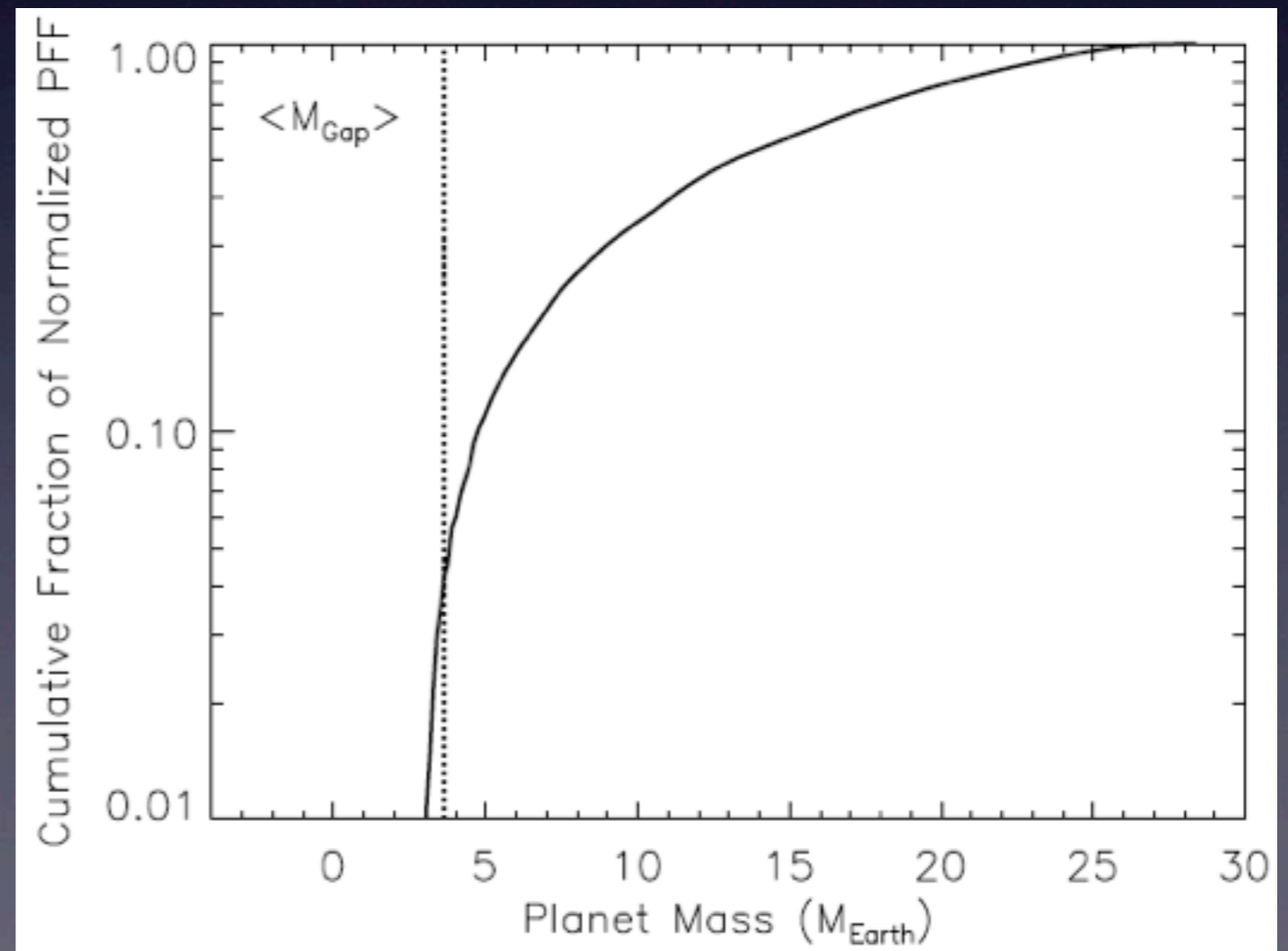
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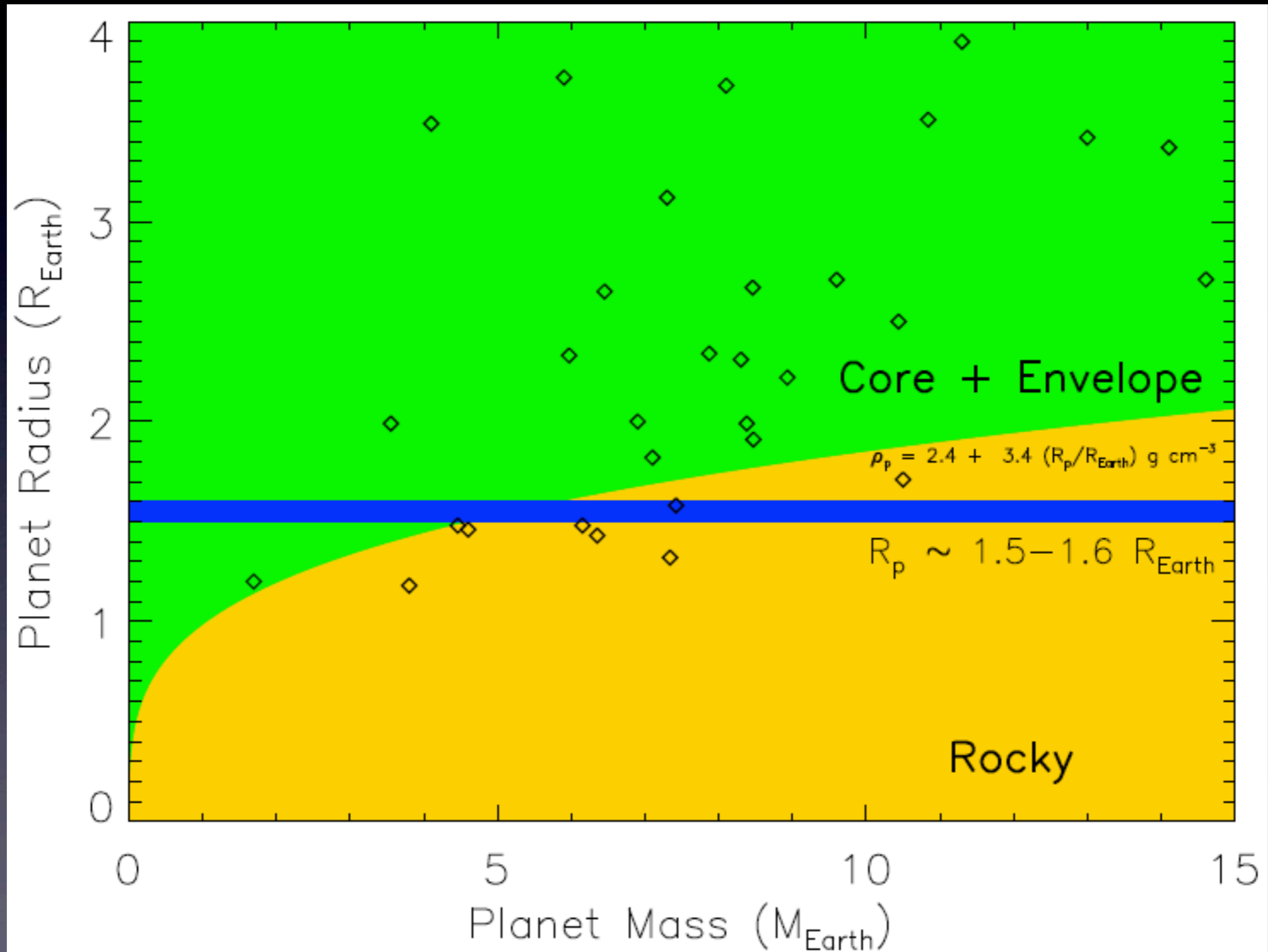
$\langle M_{Gap} \rangle$

= the mean value of
the gap-opening mass of
planets which end up
in the low-mass regime



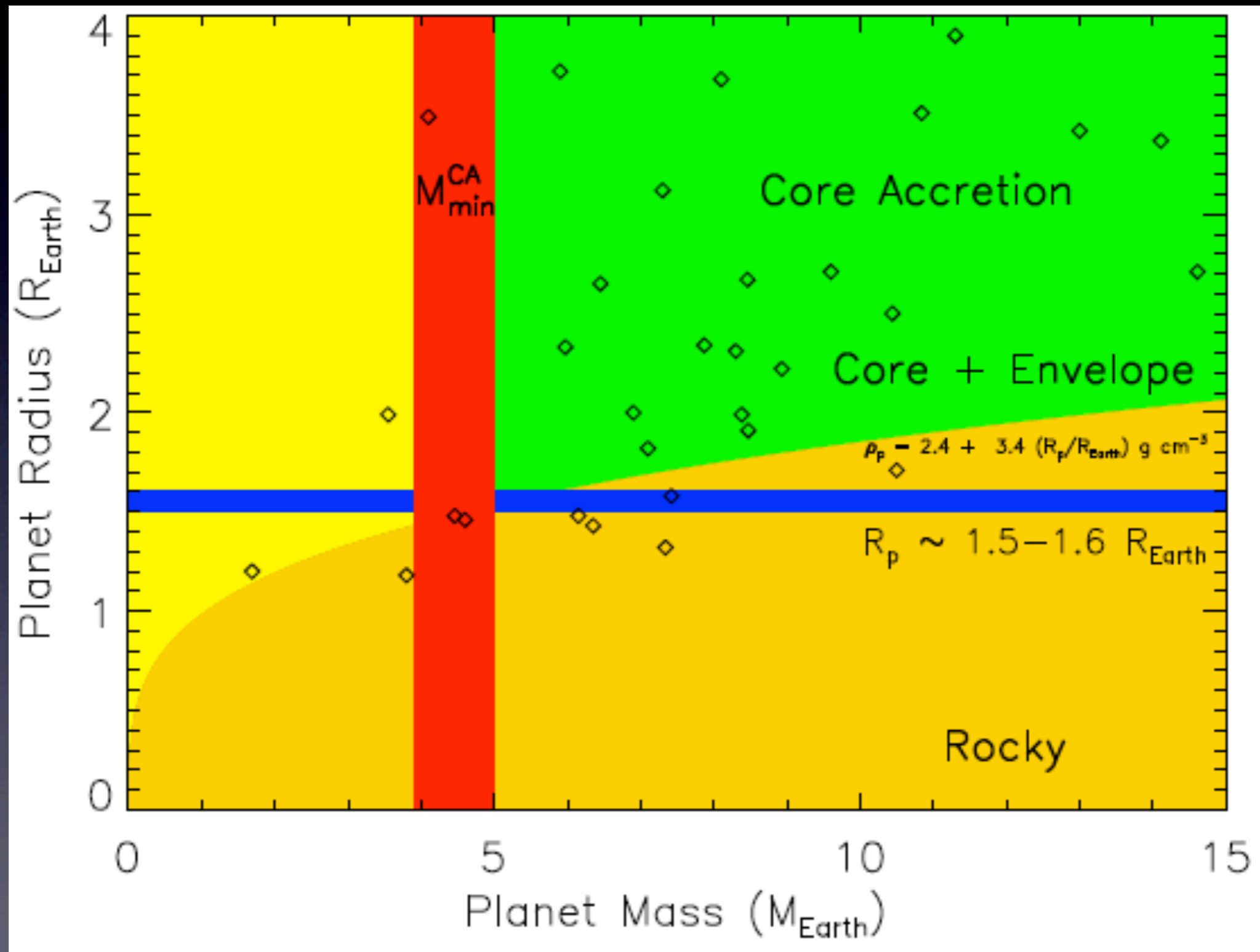
Implication for the Mass-Radius Diagram

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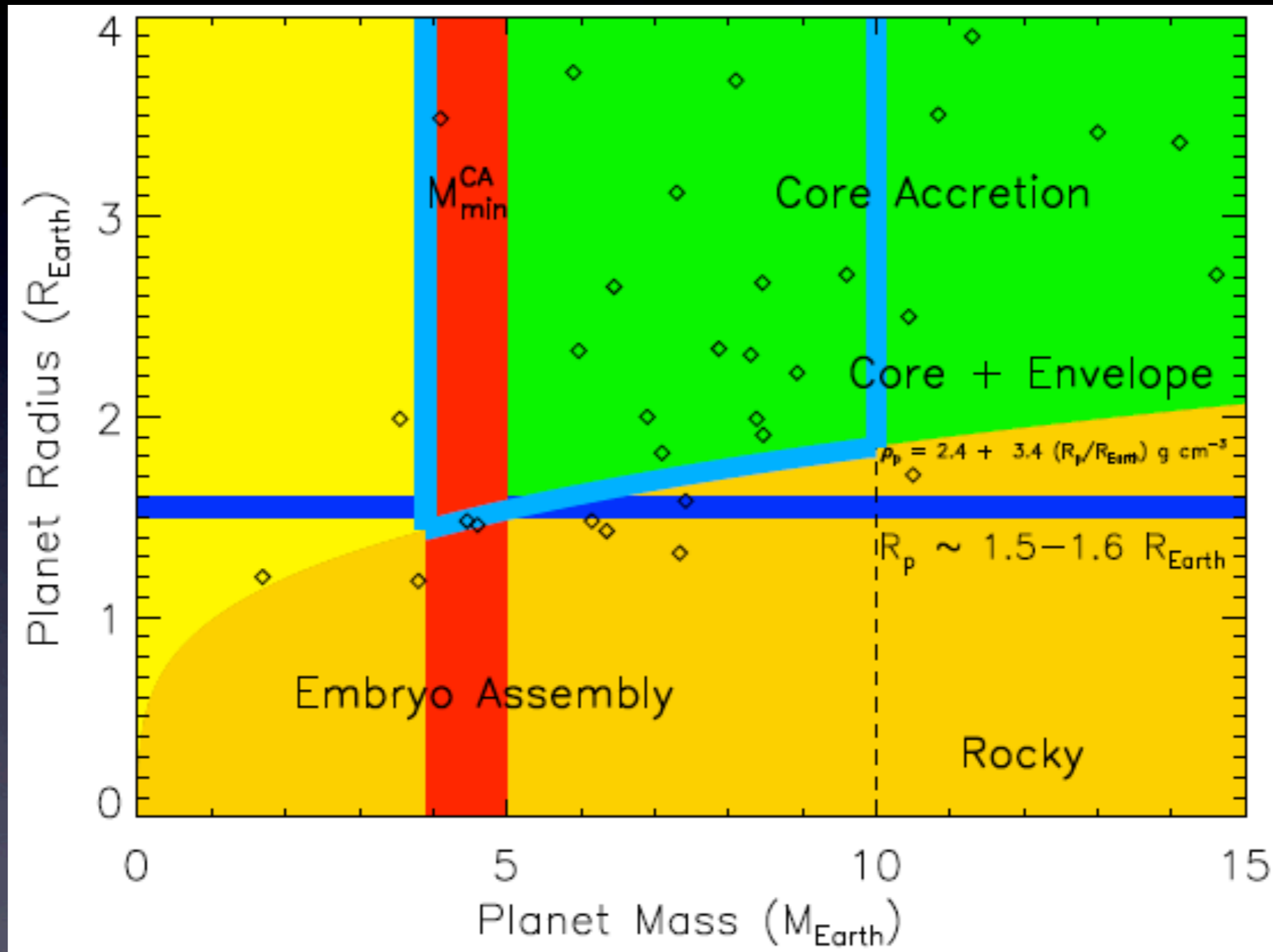
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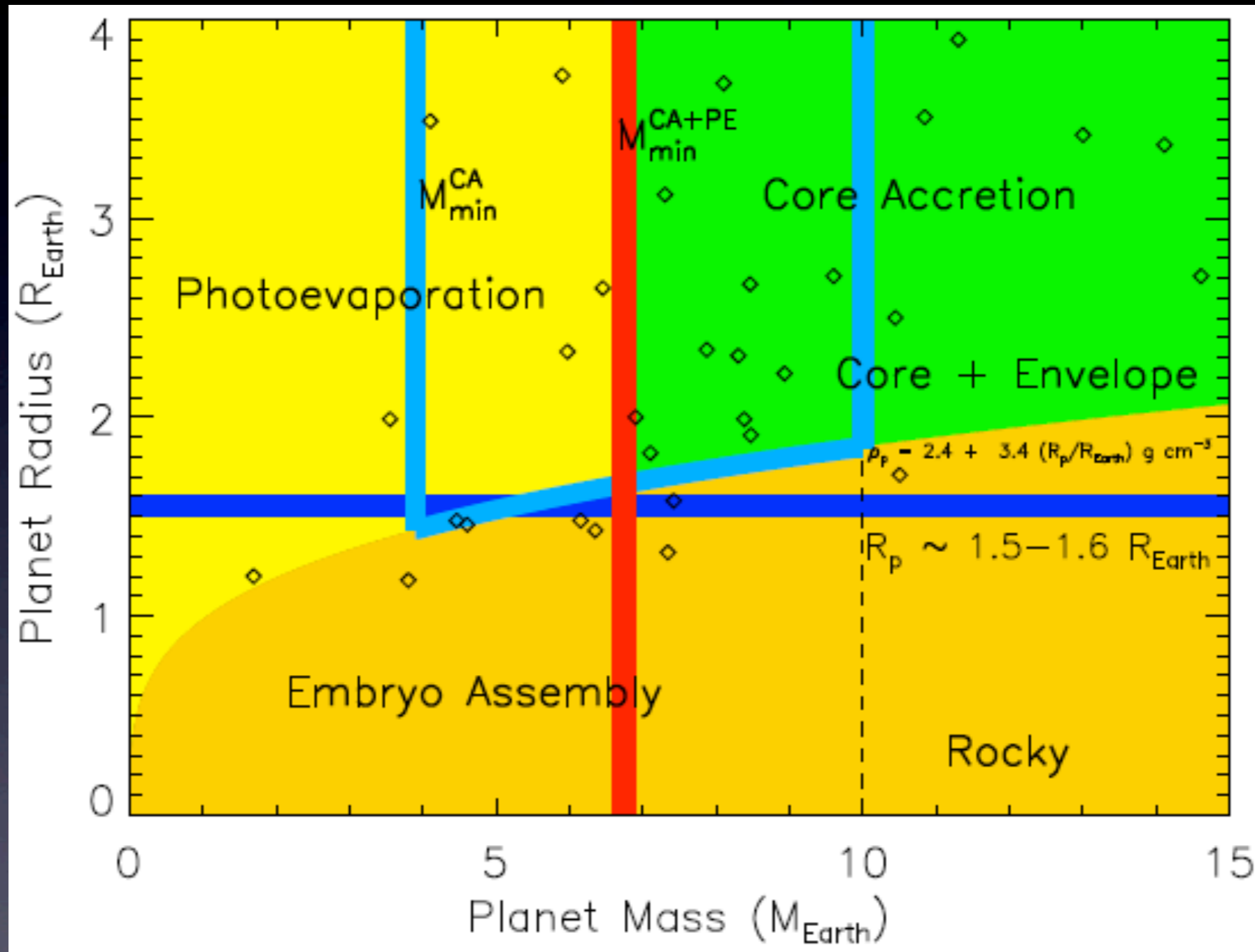


Embryo assembly scenario (in situ formation)
can form planets with $< 10 M_{\text{Earth}}$

e.g., Ogihara & Ida 2009,
Hansen & Murray 2013

Implication for the Mass-Radius Diagram

Hasegawa 2014 in prep

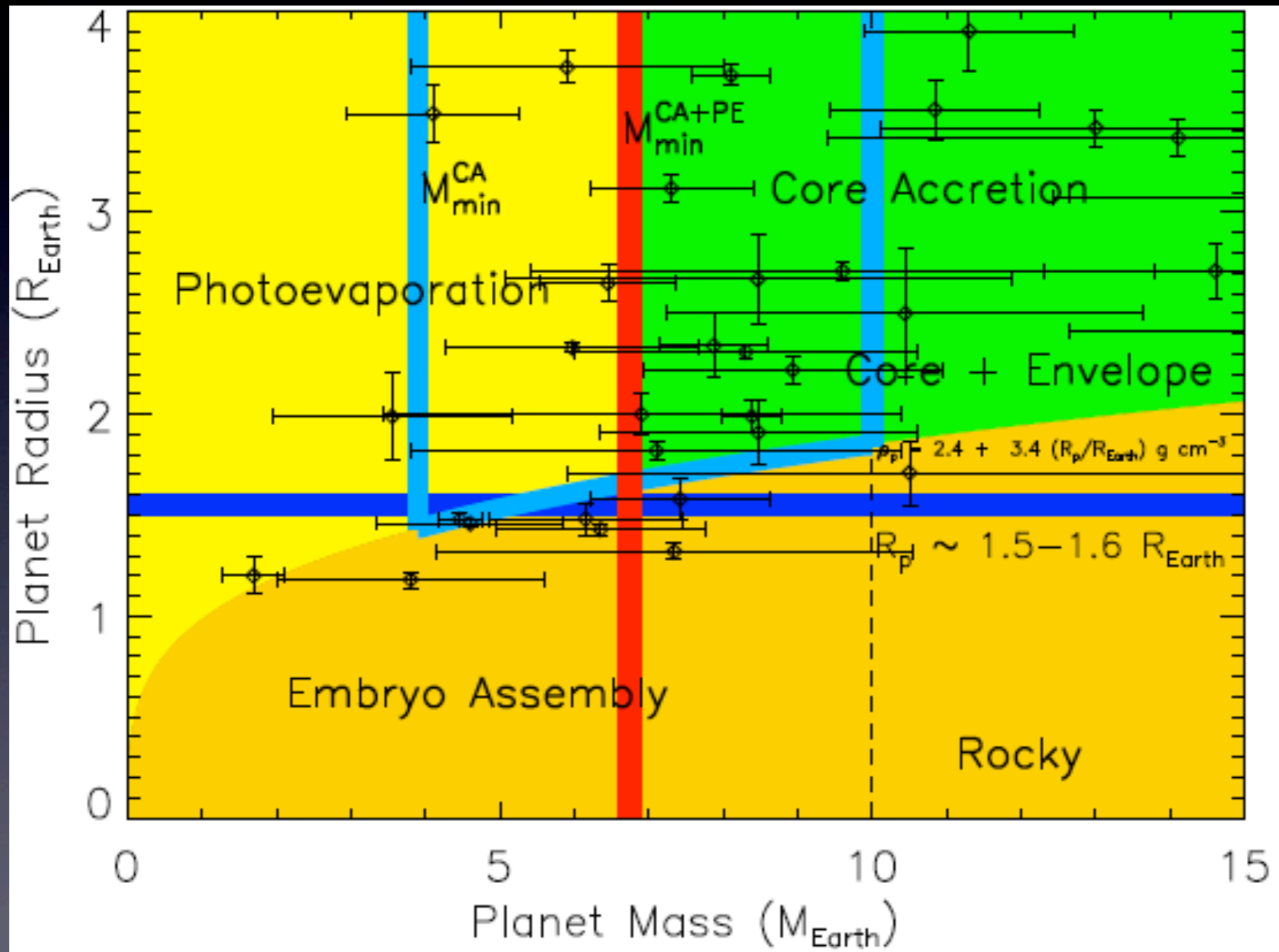


Inclusion of photoevaporative mass loss from planets

Lopez & Fortney 2013

Exoplanet “Phase” Diagram

Hasegawa 2014 in prep



Summary

- Super-Earths are very interesting populations
- The composition of super-Earths may change significantly around $R_p = 1.5 R_{\text{Earth}}$ ($M_p = 4-5 M_{\text{Earth}}$)
- Discussed a new statistical approach - PFF by combining planet traps with core accretion
- Our model suggests that the minimum mass of planets formed by our model is $M_p > 4-5 M_{\text{Earth}}$
- The results do not change very much for a certain range of parameters involved with planet formation
- Our results can be understood by intimate coupling of planet formation and migration (especially by type II)